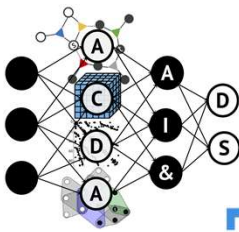


Applied and Computational Discrete Algorithms Shine in Making Sense of High-Throughput Biological Network Data: 3 Short Stories

Lenore J. Cowen
Tufts University



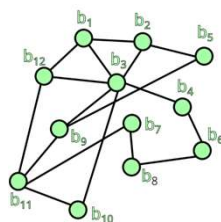
Tufts
UNIVERSITY



First Short Story: Approximate IsoRank

Global Network Alignment Problem

One of the Most Famous Problems in Network Biology:
starts with a classical PPI network



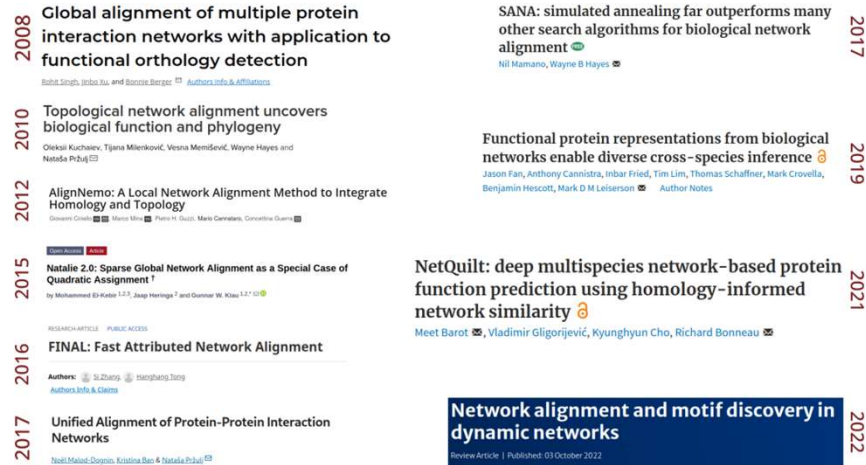
Classical PPI Network:

Vertices: proteins

Edges: these proteins physically interact

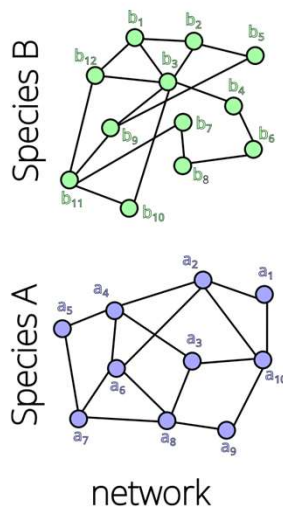
Note: undirected, unweighted or confidence weights

Network Alignment Methods Over the Years



Global Network Alignment Problem: Description

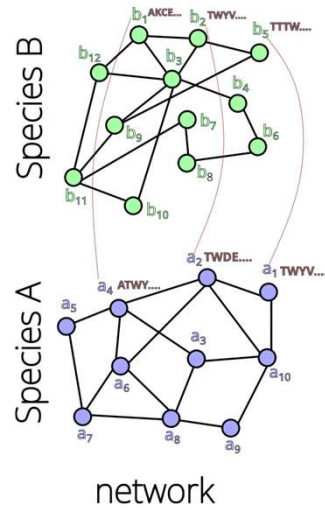
Input



network

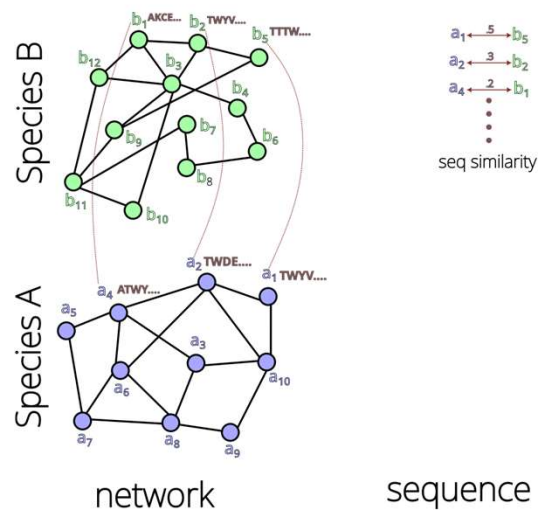
Network Alignment Problem

Input



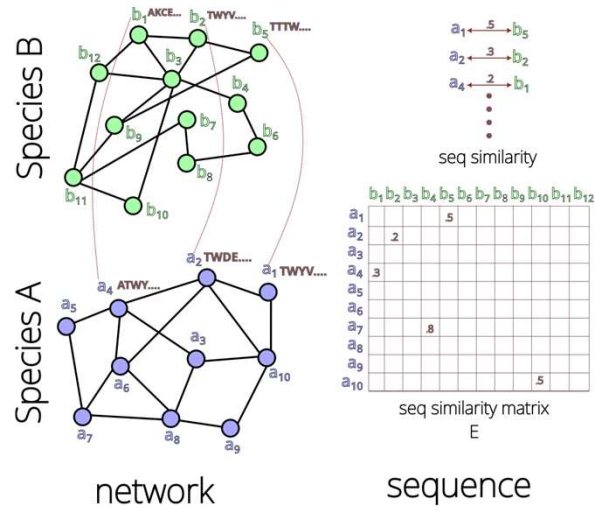
Network Alignment Problem

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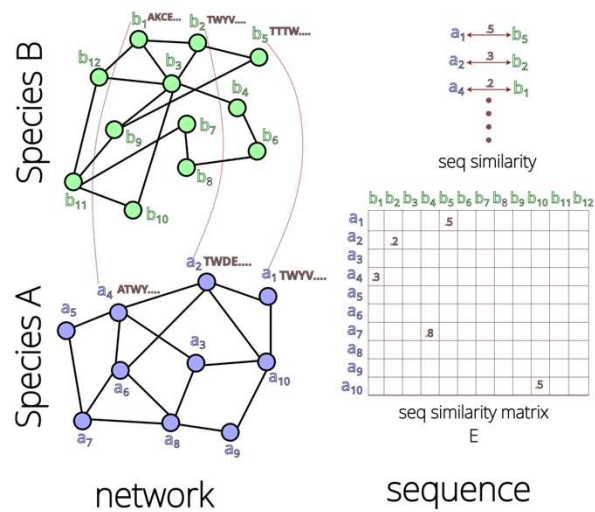
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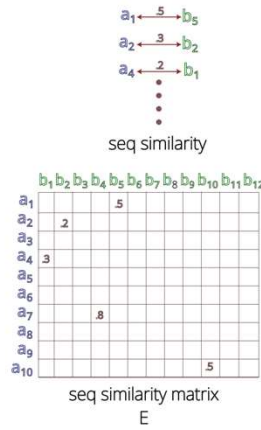
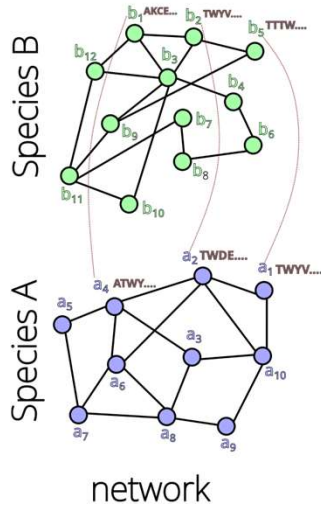


Output

Network Alignment

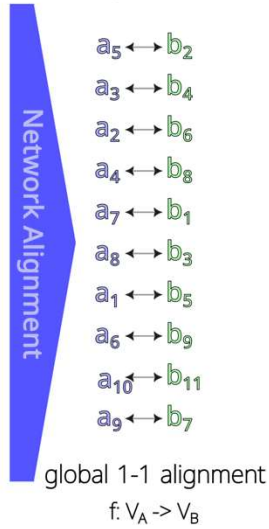
Network Alignment Problem

Input



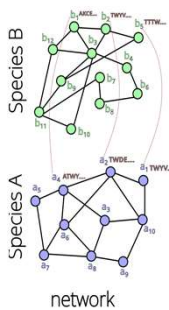
sequence

Output

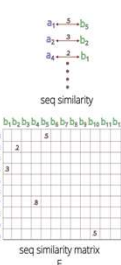


Network Alignment Problem: for functional annotation transfer

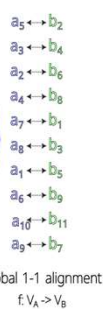
Input



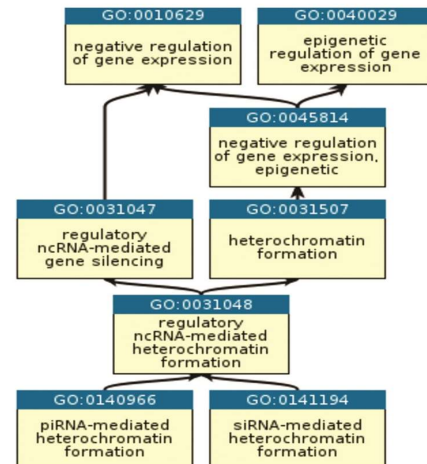
sequence



Output



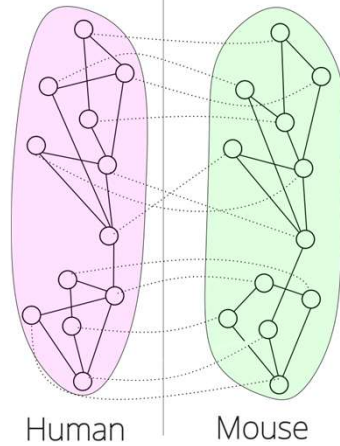
Functional annotation from GO



"The Gene Ontology knowledgebase in 2026." *Nucleic Acids Research* 54, no. D1 (2026): D1779-D1792.

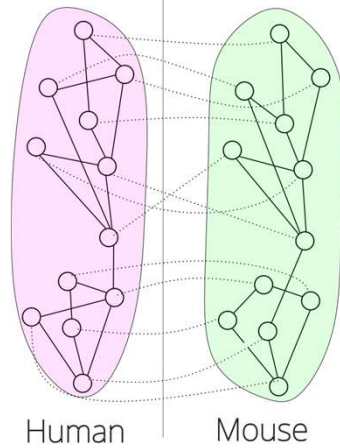
Global vs Local Network Alignment

Global One-To-One Alignment

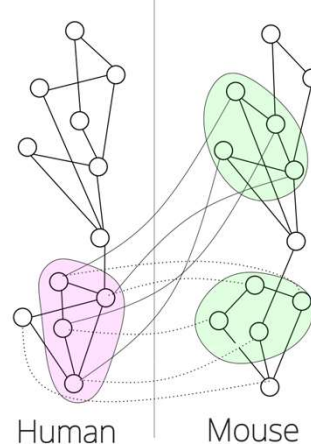


Global vs Local Network Alignment

Global One-To-One Alignment



Local Many-To-One Alignment



Classical tool: IsoRank¹

- ▶ Won the 2019 RECOMB test of time award (presented in RECOMB 2007)
- ▶ Popular global alignment algorithm that uses network structure and sequence.
- ▶ Uses spectral graph properties to find one to one alignment. **Uses the global network topology to find alignments.**
- ▶ Based on the idea that, if a node of a source PPI is aligned with node from a target PPI, their neighbors should be aligned as well

¹Singh, Rohit, Jinbo Xu, and Bonnie Berger. "Global alignment of multiple protein interaction networks with application to functional orthology detection." *Proceedings of the National Academy of Sciences* 105, no. 35 (2008): 12763-12768.

IsoRank Algorithm: Greedy Alignment

Input:

- ▶ $G_1 = (V_1, E_1),$
 $G_2 = (V_2, E_2),$ where
 $n_1 = |V_1|, n_2 = |V_2|$
- ▶ Sequence Similarity
(Optional) : $E = R^{n_1 \times n_2}$

Output:

- ▶ Network alignment matrix:

$$R \in \mathbb{R}^{n_1 \times n_2}$$

**Greedy alignment on R to
 produce $f : V_1 \rightarrow V_2$**

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	a'	b'	c'	
a	0.15	0.7	0.15	
b	0.6	0.3	0.1	$a \leftrightarrow b'$
c	0.04	0.06	0.9	$b \leftrightarrow a'$
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- Two ways of formulating IsoRank:
 1. sequence similarity not used
 2. with sequence similarity

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Greedy alignment on R to
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- The problem becomes $R = AR$ (1)

$$A_{ij}^{uv} = \begin{cases} \frac{1}{|N(u)N(v)|} & \text{if } (i, u) \in E_1, (j, v) \in E_2 \\ 0 & \text{o.w.} \end{cases}$$

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We recognize 1 as the problem of finding dominant Eigenvectors

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where, A is the **same** 4-tensor

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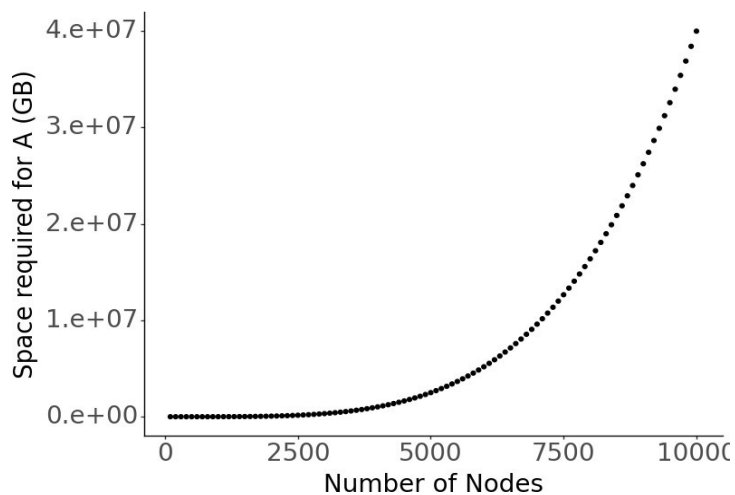
- Linear system. Iterative linear solver.

Space consideration for A

- ▶ As $A \in \mathbb{R}^{(n_1 \times n_2) \times (n_1 \times n_2)}$, the dense computation of A is unfeasible in time and space.

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Tensor Reformulation of IsoRank and its fast computation

Exact solution when no sequence similarity

- Let $A_1 \in \mathbb{R}^{n_1 \times n_1}$, $A_2 \in \mathbb{R}^{n_2 \times n_2}$ be the adjacency matrices of G_1 and G_2 respectively

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$$\begin{pmatrix} a_0 & a_1 \\ a_2 & a_3 \end{pmatrix} \otimes \begin{pmatrix} b_0 & b_1 \\ b_2 & b_3 \end{pmatrix} = \begin{pmatrix} a_0 b_0 & a_0 b_1 & a_1 b_0 & a_1 b_1 \\ a_0 b_2 & a_0 b_3 & a_1 b_2 & a_1 b_3 \\ a_2 b_0 & a_2 b_1 & a_3 b_0 & a_3 b_1 \\ a_2 b_2 & a_2 b_3 & a_3 b_2 & a_3 b_3 \end{pmatrix}$$

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- ▶ If $R = \text{vec}(R)$, $R = AR \quad (3)$

Contribution 1: Exact solution when only graph similarity considered (sequence similarity not used)

- If $d_1 = A_1 e$, $d_2 = A_2 e$, where e is an all-1 column vector

Exact solution when only graph similarity considered (sequence similarity not used)

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- If $\pi = d_1 \otimes d_2$, then

$$\begin{aligned}
 A(d_1 \otimes d_2) &= (P_1 \otimes P_2)(d_1 \otimes d_2) \\
 &= (P_1 d_1) \otimes (P_2 d_2) \\
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 \end{aligned} \tag{4}$$

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- ▶ So $\pi = d_1 \otimes d_2$ is a closed-form solution to the problem

Main Contribution: R^0 : A very good guess for IsoRank, when sequence similarity given

- ▶ IsoRank with sequence similarity:

$$R = \alpha E + (1 - \alpha)AR \quad \|E\|_1 = 1$$

Contribution 2: R^0 : A very good guess for IsoRank, when sequence similarity given

- IsoRank with sequence similarity:

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- We use the close-form solution (π) to guess the IsoRank solution, which we call R^0

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$$R = \alpha E + (1 - \alpha)AR \quad \|E\|_1 = 1$$

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$$R^0 = \alpha E + (1 - \alpha)\pi \quad (5)$$

Where recall π is the steady state solution of the tensor product graph with $\pi = \mathbf{d}/\mathbf{d}_{\text{total}}$

$$\text{And } \mathbf{d} = D\mathbf{1}_{|V_1||V_2|} \quad \text{And } \mathbf{d}_{\text{total}} = \mathbf{d}^T \mathbf{1}_{|V_1||V_2|}$$

Contribution 3: Apply 1-step IsoRank update to get intermediate IsoRank result

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- ▶ To compute AR^0 , we apply the identity

$$\begin{aligned} AR^0 &= P_1 \otimes P_2 R^0 \\ &= P_2 \text{vec}^{-1}(R^0) P_1^T \end{aligned} \quad (6)$$

- ▶ Note that, applying (6) until convergence gives us the true IsoRank R

Speedup: Construct a Barabasi-Albert random graph with $\sim 5x$ edges as vertices and a random permutation

V1, V2 = 2,500; 5,000; 10,000

E1,E2 $\sim 5V$

Speedup

V1, V2=10000

> 7 hrs

Original
Implementation

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41 seconds

~ **600 times faster**Our **R**
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~**4200 times faster**

R1

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Implementation

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~ 600 times faster

Our **R**
implementation

6 seconds

~4200 times faster

R1

3 seconds

~8400 times faster

R0

How good are R^0 and R^1 approximations?
Analysis using Synthetic Networks.

Synthetic Networks Construction

- ▶ We know the true alignment

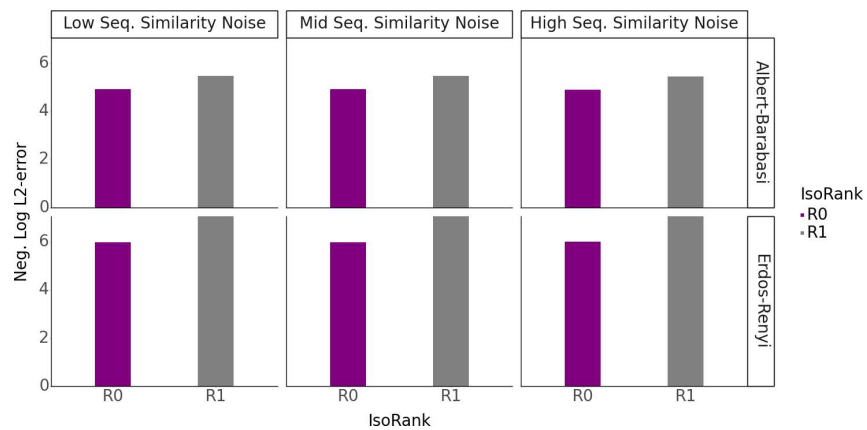
Synthetic Networks Construction

- ▶ We know the true alignment
- ▶ Introduce noise to the seq. similarity to obtain performances at different noise level.

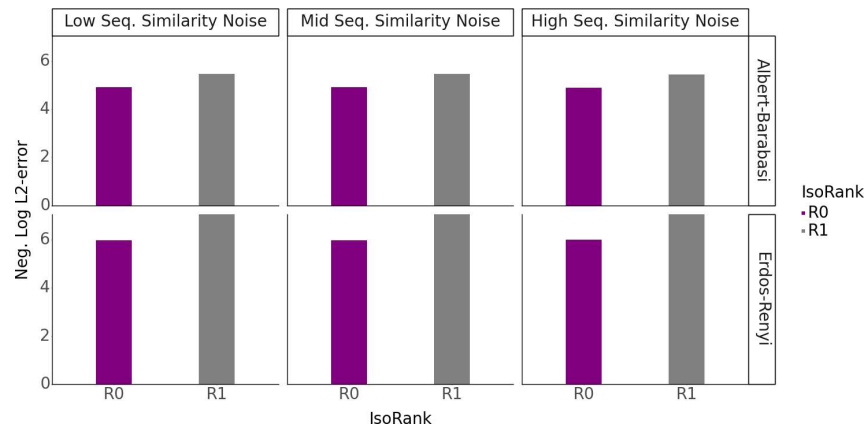
Synthetic Networks Construction

- ▶ We know the true alignment
- ▶ Introduce noise to the seq. similarity to obtain performances at different noise level.
- ▶ Used Erdős Rényi (ER) and Barabási-Albert (BA) graphs.
- ▶ How different are R^0, R^1 compared to the true R in terms of $L2$ norm?

Error Results: number of nodes = 10,000



Error Results: number of nodes = 10,000



- Turns out the approximations are really close to the true IsoRank.

Biological Networks

Biological networks

- Used IntAct database ²

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human	32431	301529	18.595	0.069
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²Noemi del Toro et al. The IntAct database: efficient access to fine-grained molecular interaction data, Nucleic Acids Research, 7 January 2022.

Evaluation Metrics for Biological Experiments

- From the R -approximations, used greedy method to find the top 2000 one-to-one mappings for analysis

Evaluation Metrics for Biological Experiments

- ▶ From the R -approximations, used greedy method to find the top 2000 one-to-one mappings for analysis
- ▶ Two types of metrics used:
 1. **Graph-theoretic**
 - ▶ How similar are the local neighborhoods produced by the global mappings?
 2. **Function-based**
 - ▶ Uses GO functional labels

Graph-theoretic methods

- ▶ Edge Correctness³: Measures if an edge in one network is also present in another network

³Hashemifar S, Xu J. HubAlign: an accurate and efficient method for global alignment of protein-protein interaction networks. *Bioinformatics*. 2014 Sep 1;30(17):i438-44. doi: 10.1093/bioinformatics/btu450. PMID: 25161231; PMCID: PMC4147903.

Graph-theoretic methods

- ▶ Edge Correctness³: Measures if an edge in one network is also present in another network
- ▶ Largest Common Connected Subgraph (LCCS): Measures the largest connected component of the transferred edges

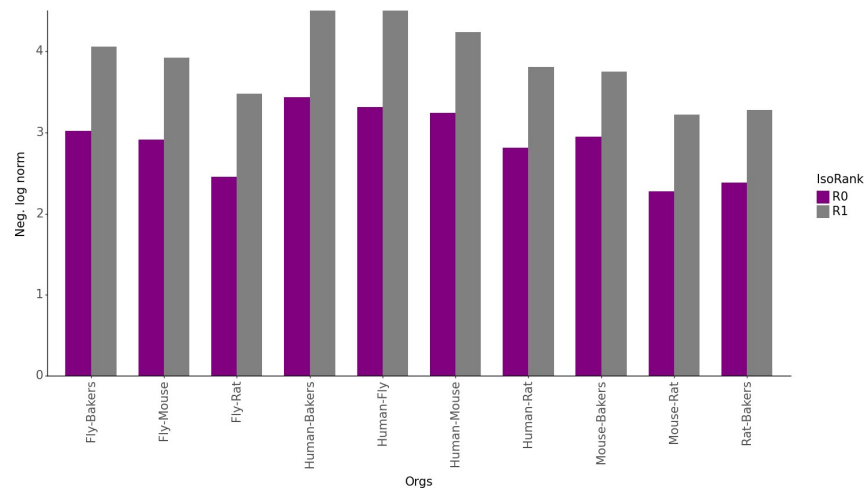
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Function-based methods

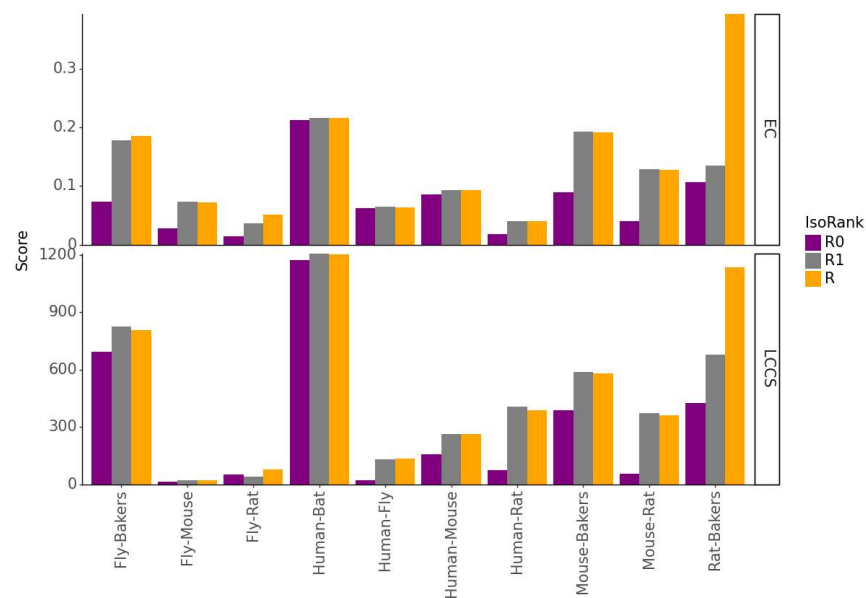
- ▶ Average Functional Similarity (AFS): Measures the average Schlicker's similarity⁴ between the one-one couplings obtained.
- ▶ We used all three GO hierarchies.

⁴A. Schlicker, F. S. Domingues, J. Rahnenführer, and T. Lengauer. A new measure for functional similarity of gene products based on gene ontology. *BMC bioinformatics*, 7(1):1–16, 2006.

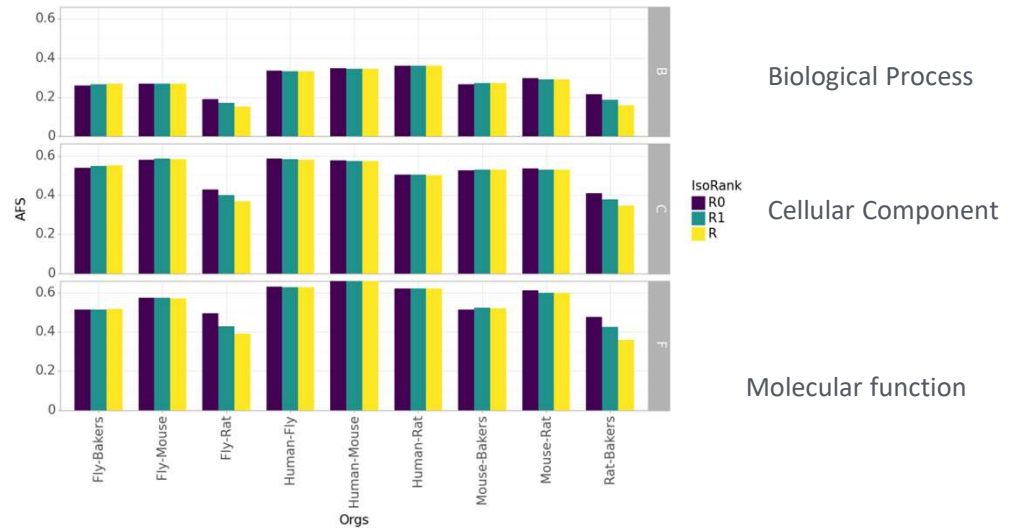
Approximation Results on Biological Network - Norms



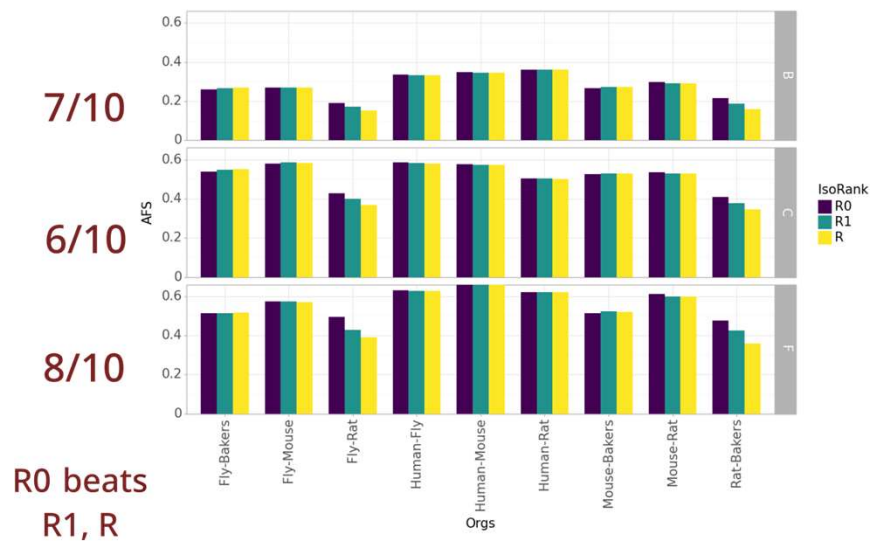
Network measures on Biological Network - EC & LCCS



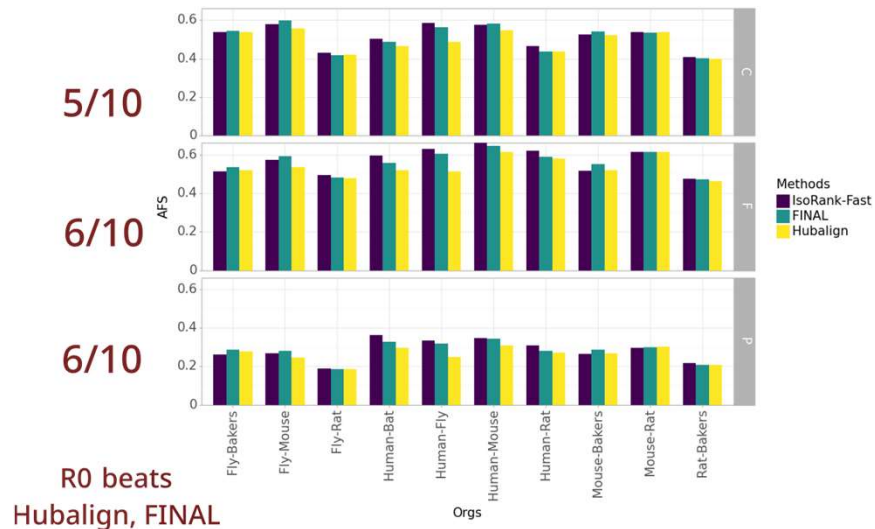
Function-based measures on Biological Network - *AFS*



Function-based measures on Biological Network - *AFS*



Function-based comparisons with competing methods- AFS



Summary

- ▶ The scalability of original IsoRank deteriorated with the number of nodes
- ▶ We propose an exact very-fast algorithm for IsoRank (when sequence information not used)
- ▶ Very fast and functionally informative guess R^0 , when sequence similarity provided.
- ▶ One step update on R^0 to produce an approximation closer to IsoRank (called R^1)
- ▶ R^0 outperforming R^1 and true IsoRank R on biological networks, when function based metric was used for comparison.

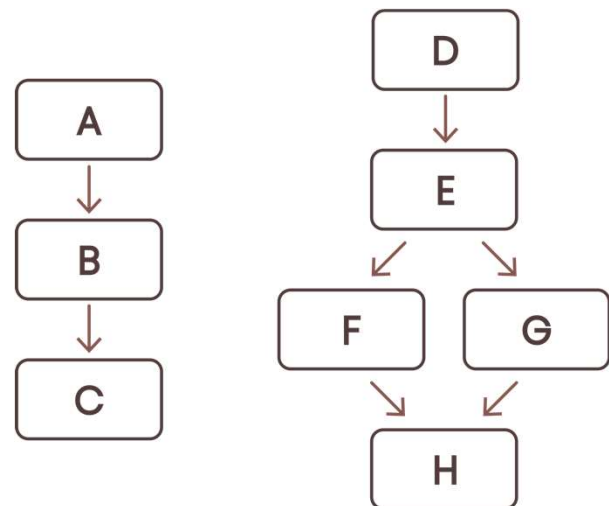
Compensatory Pathways in Genetic Interaction Networks:

A different kind of interaction network



What is a compensatory pathway?

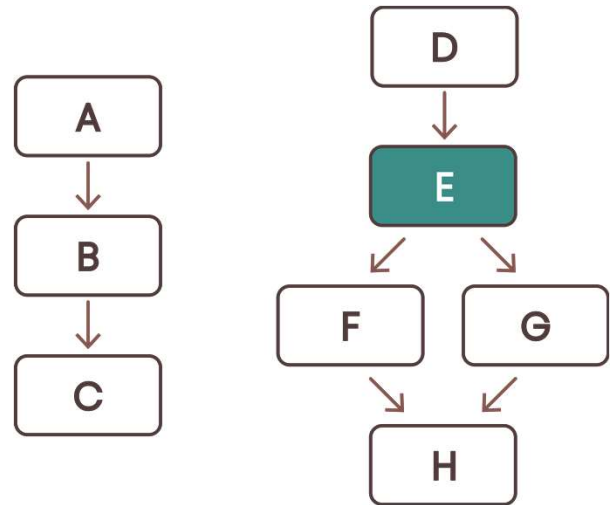
Imagine that essential DNA repair can be performed by two distinct cell pathways



What is a compensatory pathway?

Imagine that essential DNA repair can be performed by two distinct cell pathways

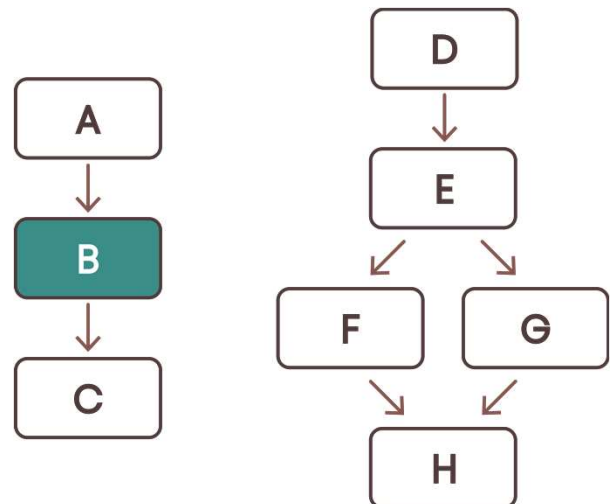
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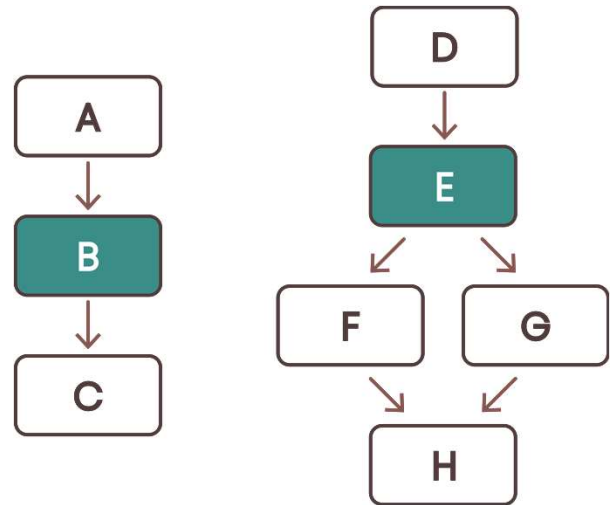
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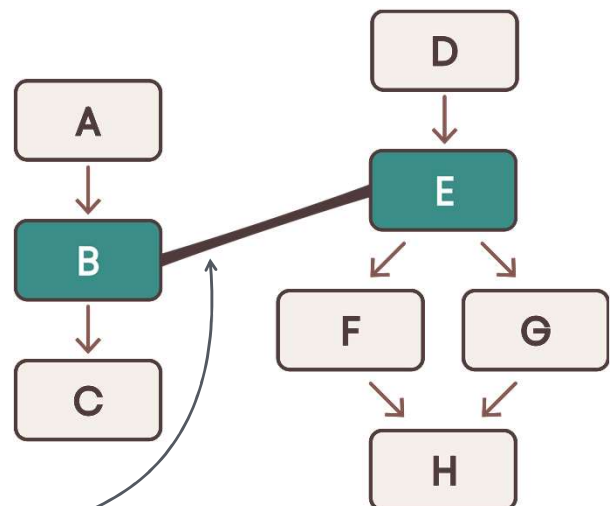
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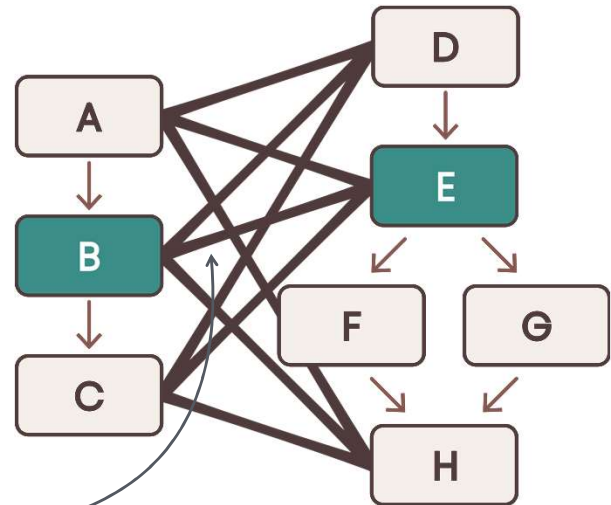


These are **synthetic lethality** interactions
(gene pairs that only cause cell death together)

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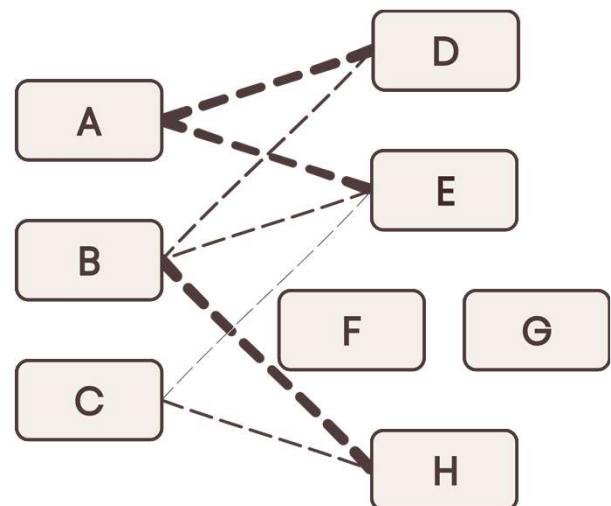
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Synthetic Lethality → Synthetic Sickness

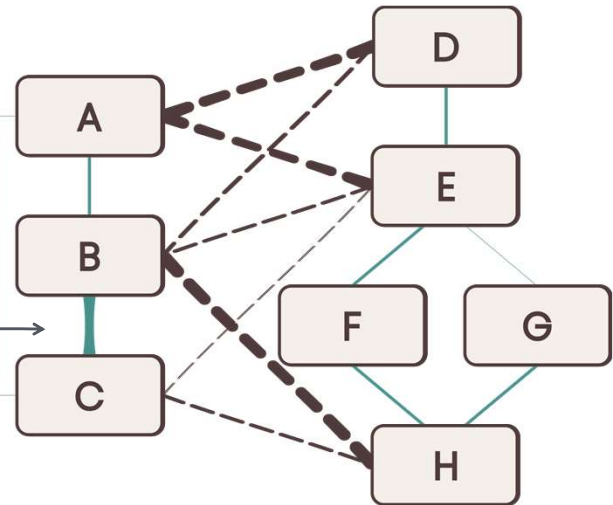
We can expand from binary interactions to *synthetic sickness*, a weighted edge where the cell is sicker than expected



Synthetic Lethality → Synthetic Sickness

We can expand from binary interactions to *synthetic sickness*, a weighted edge where the cell is **sicker** than expected

...and **genetic suppression**, for when the cell is healthier than expected (which are milder)

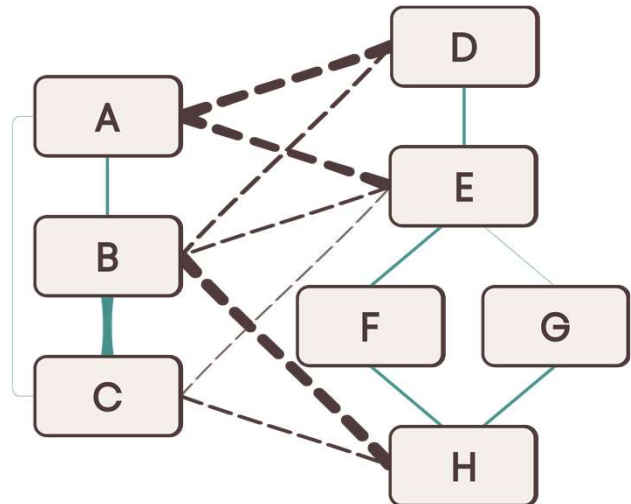


The Between Pathway Model

We call this motif a BPM because, if two **modules** (genes sets) represent compensatory pathways, they should have:

- Many synthetic sickness (**negative**) edges across pathways
- Many genetic suppression (**positive**) edges within pathways

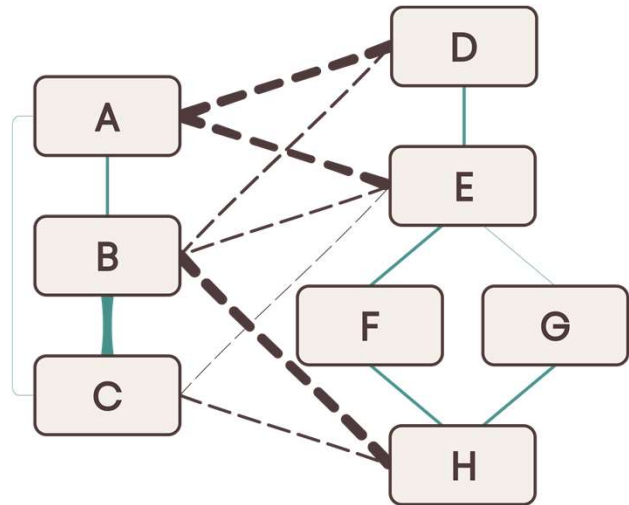
A *cohesive* BPM should contain genes in each module with **related functions**



Genetic Interaction Network → BPM

Our goal is to identify BPMs from a genetic interaction network, which is a graph where

- Nodes are nonessential genes
- Edges are weighted negative/positive genetic interactions



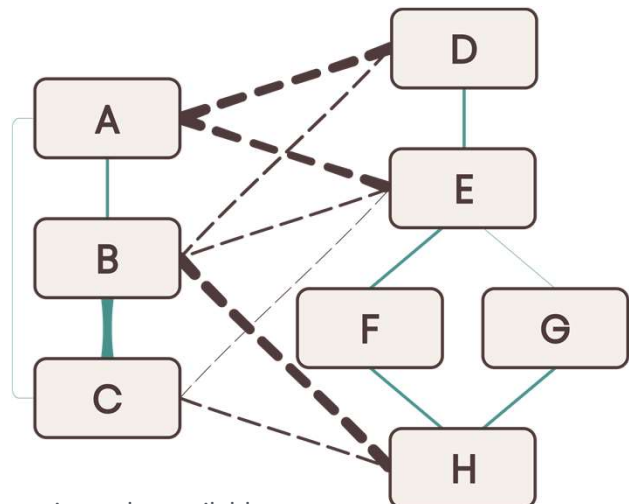
Genetic Interaction Network → BPM

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Currently we have high-throughput experiments on

Non-essential yeast genes; other organisms more data is starting to be available

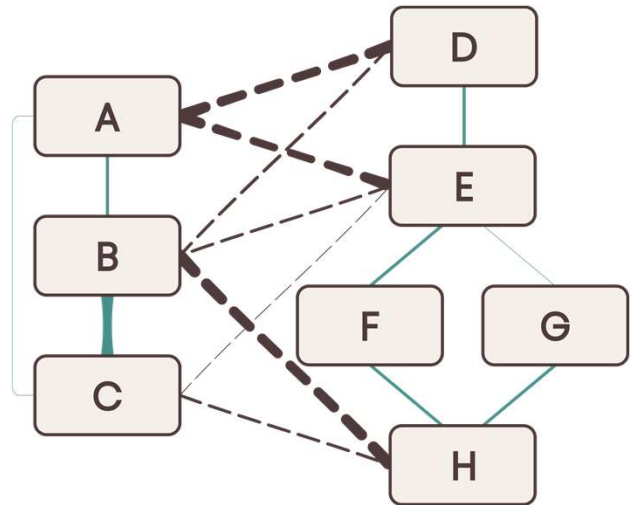


Genetic Interaction Network → BPM

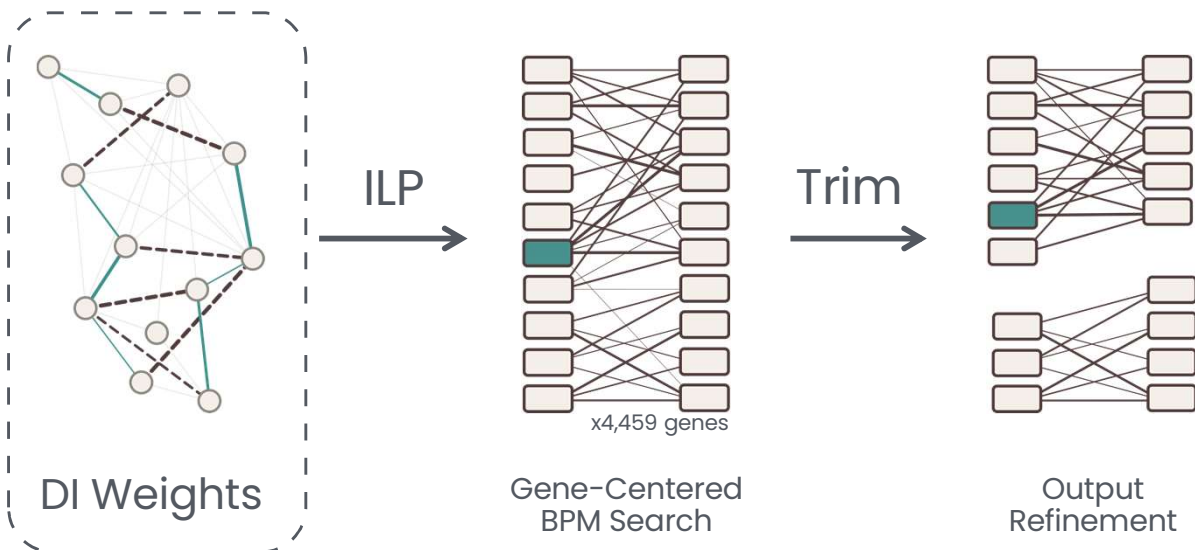
Our goal is to identify BPMs from a genetic interaction network, which is a graph where

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...but identified BPMs are only as good as the underlying network

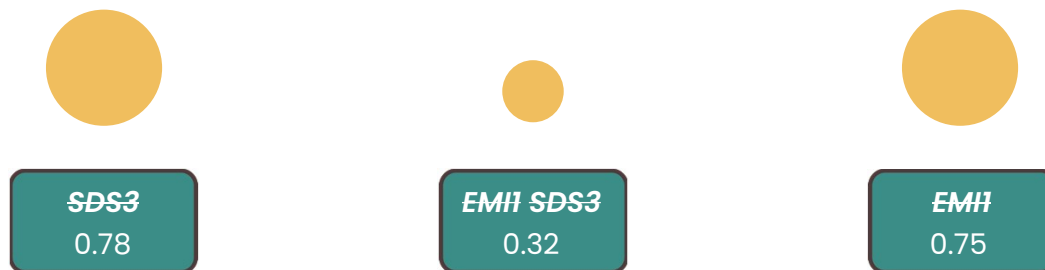


GIDEON Method Outline



Defining Genetic Interactions

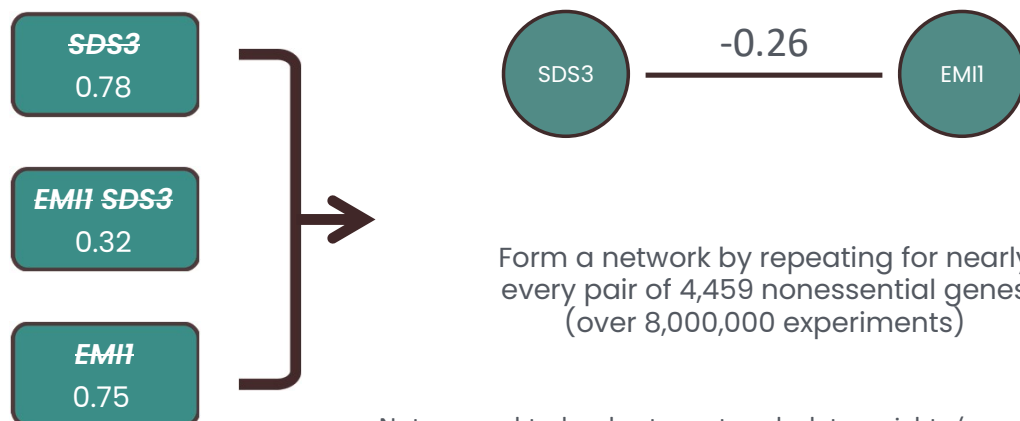
How do we quantify “sicker/healthier than expected” for the edge weights between a pair of genes? Consider *SDS3* and *EMI1*:



Compare the fitness (size) of the yeast colony under the three knockout conditions

Defining Genetic Interactions

How do we quantify “sicker/healthier than expected” for the edge weights between a pair of genes? Consider *SDS3* and *EMI1*:



Form a network by repeating for nearly every pair of 4,459 nonessential genes (over 8,000,000 experiments)

Not covered today: best way to calculate weights (see our paper)

Costanzo, Michael, et al. "A global genetic interaction network maps a wiring diagram of cellular function." *Science* 353.6306 (2016): aaf1420.

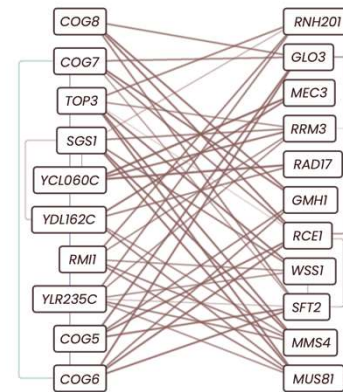
Goal: from the signed weighted genetic interaction network, discover BPMs

Two ways to measure BPM quality:

1. *Graph theoretic*
2. *Functional ENRICHMENT*

Biologists have manually annotated genes with GO terms that represent gene functions (i.e. apoptotic process). If a module has more genes with a GO term than expected by random chance, the module is enriched for that GO term.

Translation
(GO:0007049)



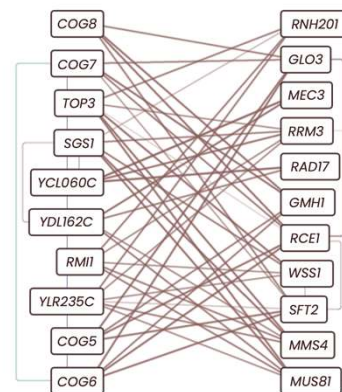
Evaluating BPMs Using Enrichment

Group BPM into four categories:

- Modules enriched for the same term
- Modules enriched for different terms
- One module enriched
- Neither modules enriched

DNA Repair (GO:0006281)

Translation (GO:0007049)



Evaluating BPMs Using Enrichment

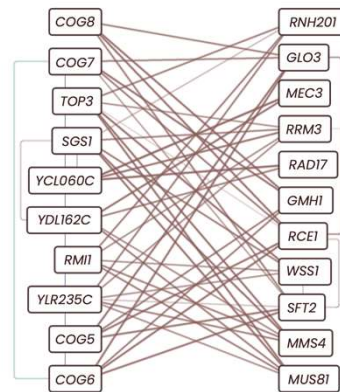
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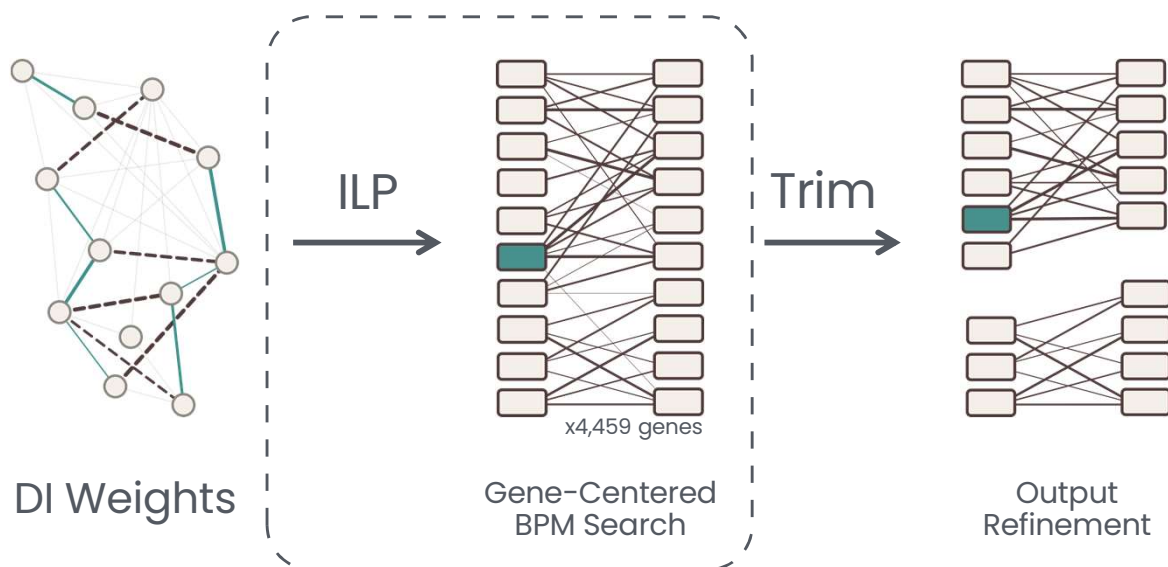
DNA Repair (GO:0006281)

Translation (GO:0007049)

Note: Annotations are incomplete and unenriched modules or unannotated genes may suggest new biological functions



GIDEON Method Outline

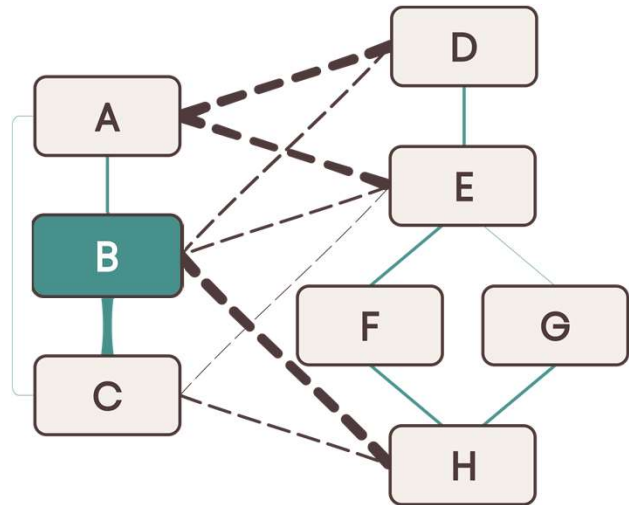


BPM Finding as Optimization

Objective: For every gene, maximize the interaction weight of a BPM containing the gene where each module has 25 genes

Interaction Weight: LocalCut approach to quantify “negative across and positive within” while accounting for BPM size

$$\frac{\sum \text{Interactions within sets} - \sum \text{Interactions between sets}}{\text{Number of Genes in BPM}}$$

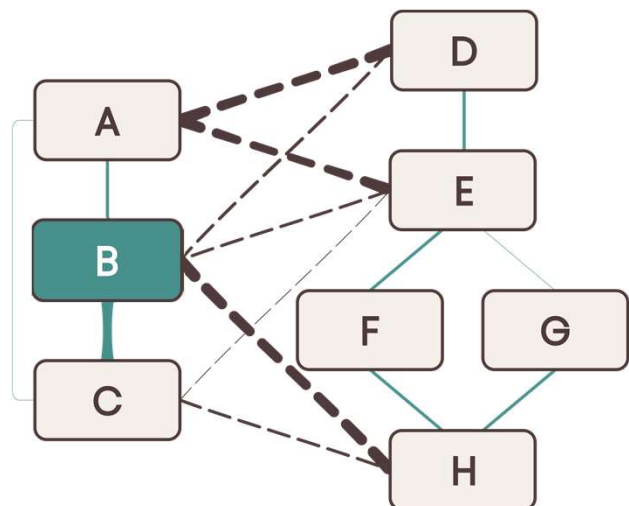


Defining the ILP for BPM Search

Let's view the location of a node n using a set of three binary variables:

$$o_n, \ell_n, r_n \in \{0,1\}$$

representing if n is in the *left* module, *right* module, or *outside* of the BPM



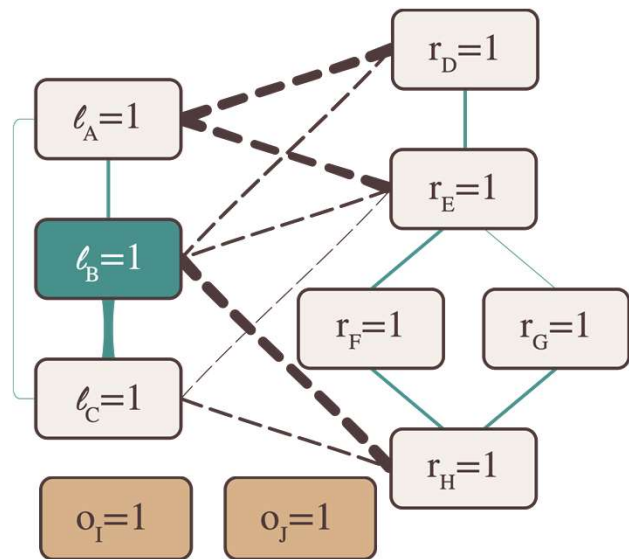
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We also need the following constraints:

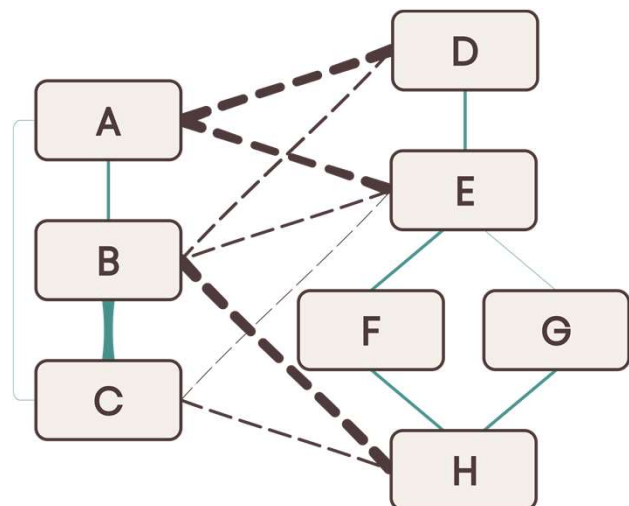
$$o_n + \ell_n + r_n = 1 \quad \ell_B = 1$$



Defining the ILP for BPM Search

To calculate the objective function, we need binary variables for every edge:
 $s_e, b_e \in \{0,1\}$

representing if e is in an edge within the *same* BPM modules or *between* BPM modules



Defining the ILP for BPM Search

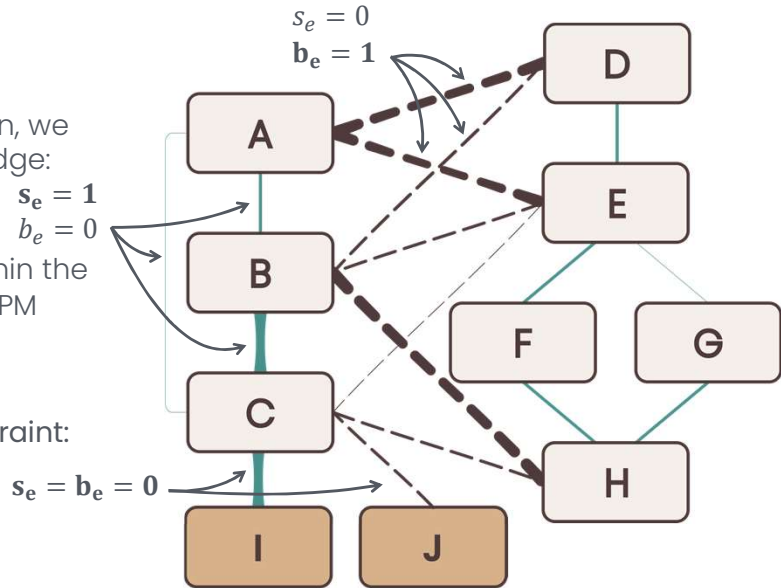
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representing if e is in an edge within the *same* BPM modules or *between* BPM modules

We also need the following constraint:

$$s_e + b_e \leq 1$$



Edge Variables $\longleftrightarrow$ Nodes Variables

Edge variables must correspond to the node variables. For an edge $e = (u, v)$:

- If the nodes are in **different** modules, then $s_e = 0$ and $b_e = 1$
- If **both** nodes are in the **same** module, then $s_e = 1$ and $b_e = 0$
- If **either** node is outside the bpm, then $b_e = s_e = 0$

Actual ILP Constraints

$$r_u + \ell_v - 1 \leq b_{(u,v)}$$

$$r_v + \ell_u - 1 \leq b_{(u,v)}$$

$$r_u + r_v - 1 \leq s_{(u,v)}$$

$$\ell_u + \ell_v - 1 \leq s_{(u,v)}$$

$$w_{(u,v)} + b_{(u,v)} \leq 1 - o_u$$

$$w_{(u,v)} + b_{(u,v)} \leq 1 - o_v$$

The ILP for BPM Searching

maximize interaction weight

Variables

For $n \in V$:

$$r_n \in \{0,1\}$$

$$\ell_n \in \{0,1\}$$

$$o_n \in \{0,1\}$$

For $e \in E$:

$$b_e \in \{0,1\}$$

$$s_e \in \{0,1\}$$

Constraints

Each module has 25 genes, each gene has 1 location, & the gene center is included

Edge variables align with node locations

$$\sum_{e \in E_n} w_e \cdot (s_e - b_e) \leq \sum_{e \in E_g} w_e \cdot (s_e - b_e)$$

$$\sum_{e \in E_g} w_e \cdot b_e \leq \sum_{e \in E_n} w_e \cdot b_e$$

The ILP for BPM Searching

maximize $\sum_{(u,v) \in E} w_{(u,v)} \cdot (s_{(u,v)} - b_{(u,v)})$

Variables

For $n \in V$:

$$r_n \in \{0,1\}$$

$$\ell_n \in \{0,1\}$$

$$o_n \in \{0,1\}$$

For $e \in E$:

$$b_e \in \{0,1\}$$

$$s_e \in \{0,1\}$$

Constraints

$$\ell_n + r_n + o_n = 1$$

$$\sum_{n \in V} \ell_n = 25$$

$$\sum_{n \in V} r_n = 25$$

$$\ell_g = 1$$

$$r_u + \ell_v - 1 \leq b_{(u,v)}$$

$$r_v + \ell_u - 1 \leq b_{(u,v)}$$

$$r_u + r_v - 1 \leq s_{(u,v)}$$

$$\ell_u + \ell_v - 1 \leq s_{(u,v)}$$

$$\sum_{e \in E_n} w_e \cdot (s_e - b_e) \leq \sum_{e \in E_g} w_e \cdot (s_e - b_e)$$

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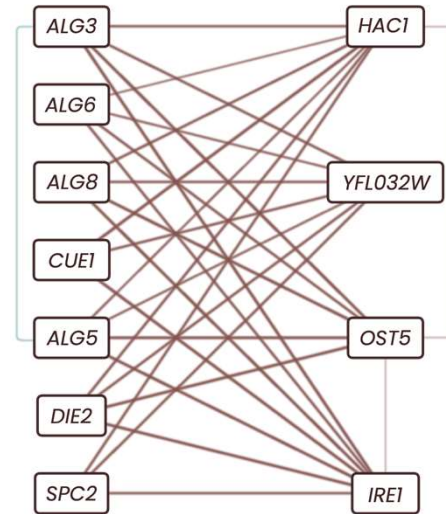
$$w_{(u,v)} + b_{(u,v)} \leq 1 - o_u$$

$$w_{(u,v)} + b_{(u,v)} \leq 1 - o_v$$

Spotlights in the Response Surface

A small set of BPMs in the search space have **huge** interaction weights

The maximum interaction weight BPM containing *IRC20* (which only has weak interactions) **disregards** its interactions

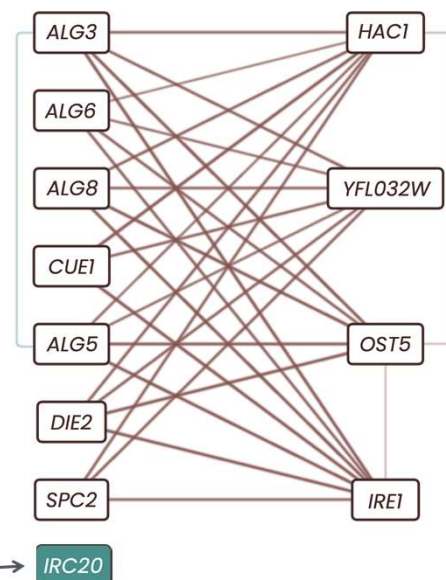


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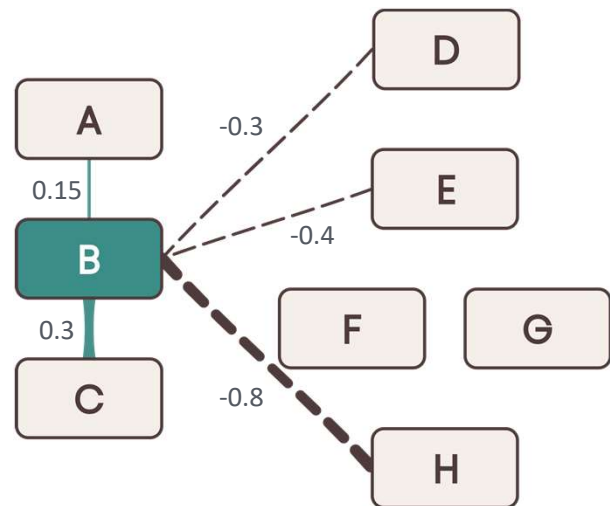
The ILP appends these genes to strong BPMs



Enforcing Local Search: *Gene* Interaction Weight

For each gene, compute the interaction weight only using its adjacent edges

$$iw_B = \frac{(0.3 + 0.15) - (-0.8 + -0.3 + -0.4)}{8} = 0.23$$



Gene-Centered Constraints

Mathematically, *some* BPM gene must have the largest "gene interaction weight"

Constraints can ensure that the gene used to build the BPM is that primary contributor to the interaction weight



Gene-Centered Constraints

Mathematically, *some* BPM gene must have the largest “gene interaction weight”

Constraints can ensure that the gene used to build the BPM is that primary contributor to the interaction weight

...and this doesn't remove any BPMs from the search space!



ILP Solvers are NOT All-Powerful

Computational Limits

- Use the No Relaxation Heuristic (powerful for combinatorial ILPs), which pieces together sub-ILPs
- Return best feasible solution within a computational limit (~400 s)



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GUROBI
OPTIMIZATION

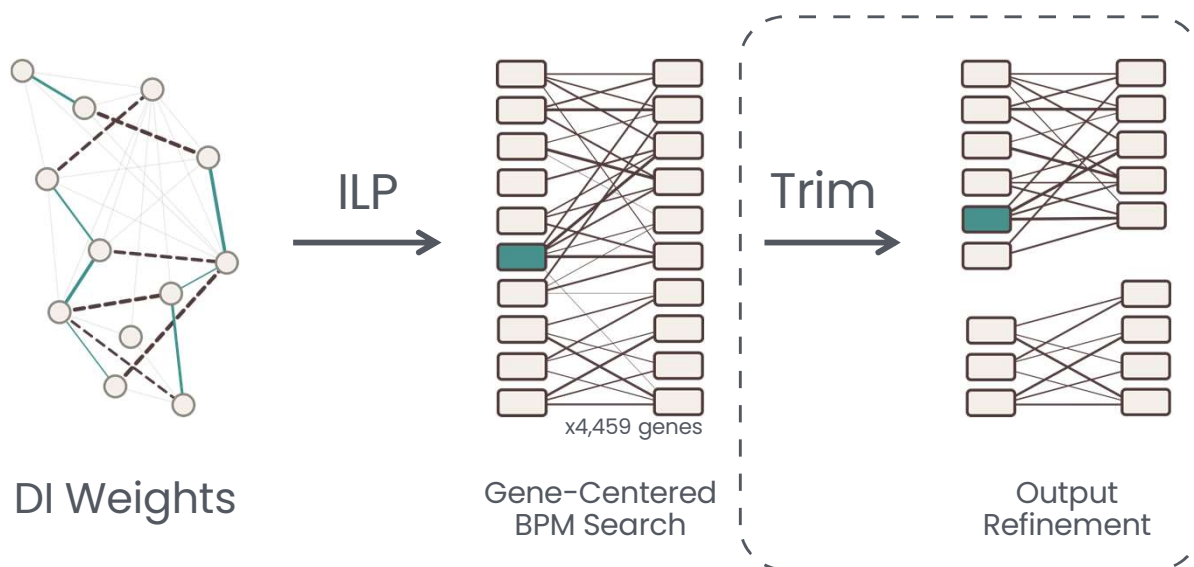
ILP Formulation Matters

- Liang et. al. maximized only the **negative weight across the BPM**
- After a BPM is found, they remove all its edges from the network and rerun the ILP (fully sequential)

An Algorithm to Mine Therapeutic Motifs for Cancer From Networks of Genetic Interactions

Publisher: IEEE | Cite This | PDF
Herty Liang ; Yu Lin ; Anand Jeyasekharan ; Vaibhav Rajan | All Authors

GIDEON Method Outline



Interaction Weight is a Nonlinear Objective

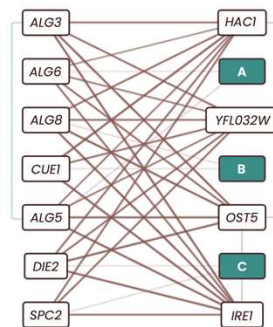
maximize interaction weight

≠

$$\text{maximize } \sum_{(u,v) \in E} w_{(u,v)} \cdot (s_{(u,v)} - b_{(u,v)})$$

$$\frac{\sum \text{Interactions within sets} - \sum \text{Interactions between sets}}{\text{Number of Genes in BPM}}$$

Larger graphs have larger edge weight sums, which LocalCut accounted for using the BPM size divisor



Without a divisor, BPMs are always the maximum allowed size because at least some of the 4,459 genes slightly improve the objective

Solution: 25 genes per module instead of 3 to 25

Initial Trimming Algorithm

Iteratively remove weakly included genes until all genes in the BPM satisfy these requirements:

1. Gene interaction weight of at least 0.015
2. At least two negative interactions across modules



Initial Trimming Algorithm

Iteratively remove weakly included genes until **all** genes in the BPM satisfy these requirements:

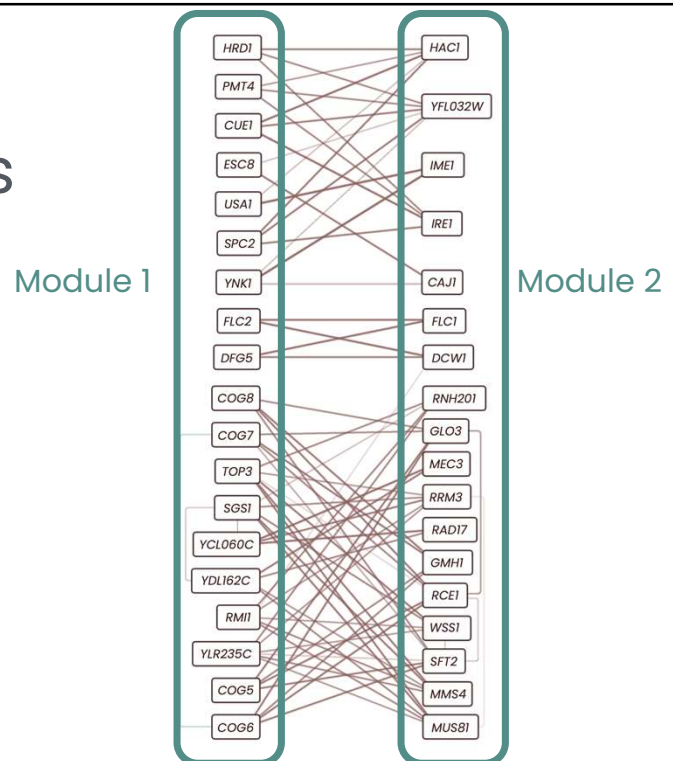
1. Gene interaction weight of at least 0.015
2. At least two negative interactions across modules

Poor BPMs centered on genes with weak interactions **lose all genes** and are naturally filtered out



Final Trim: Splitting Disconnected BPMs

Merged BPMs perform well under the objective function and survive the initial trimming process



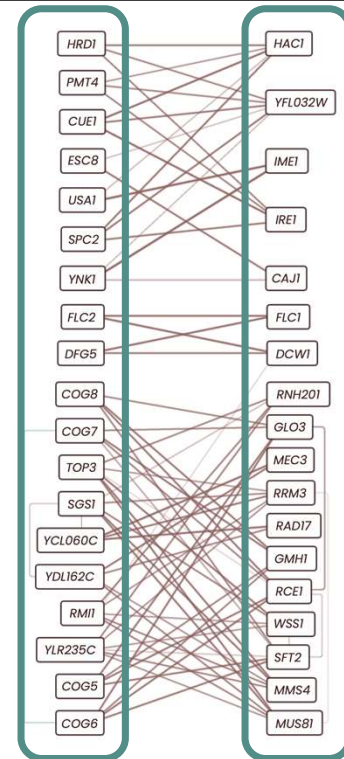
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Final Trim: After removing weak edges ($|\epsilon| < 0.2$), connected components with at least 3 genes in each module become their own BPM

Module 1

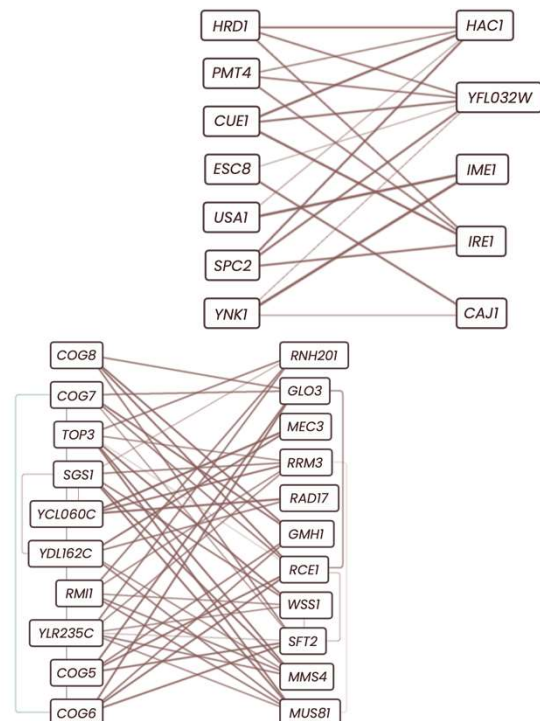
Module 2



Final Trim: Splitting Disconnected BPMs

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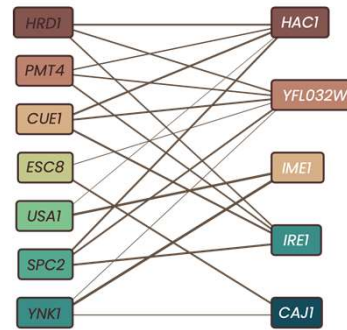


LocalCut Pruning for BPM Diversity

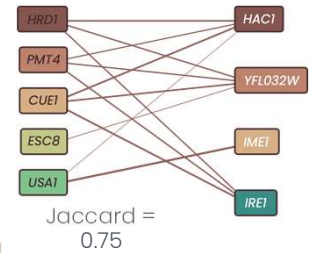
GIDEON uses the LocalCut approach to ensure the final BPM set is diverse

Method: In order of interaction weight, add a BPM A to the result set if **different enough** from all previously added BPMs B:

$$\text{Jaccard Index: } \frac{A \cap B}{A \cup B} < 0.66$$

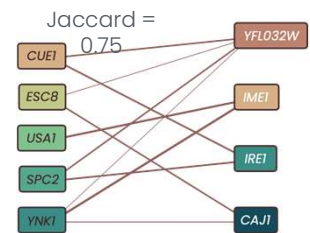


If we already have this BPM...



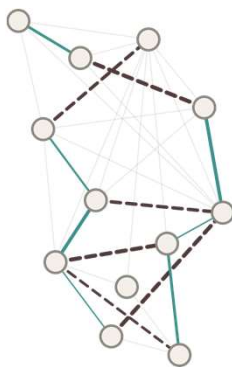
Jaccard = 0.75

...then don't add either of these



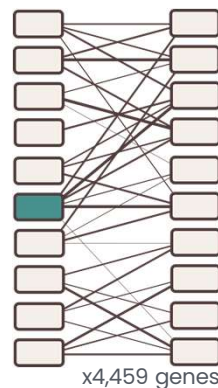
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GIDEON Method Outline



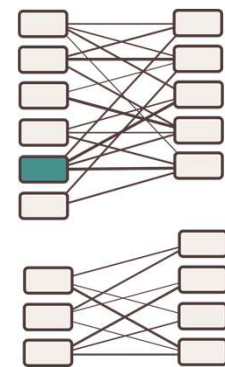
DI Weights

ILP



Gene-Centered
BPM Search

Trim

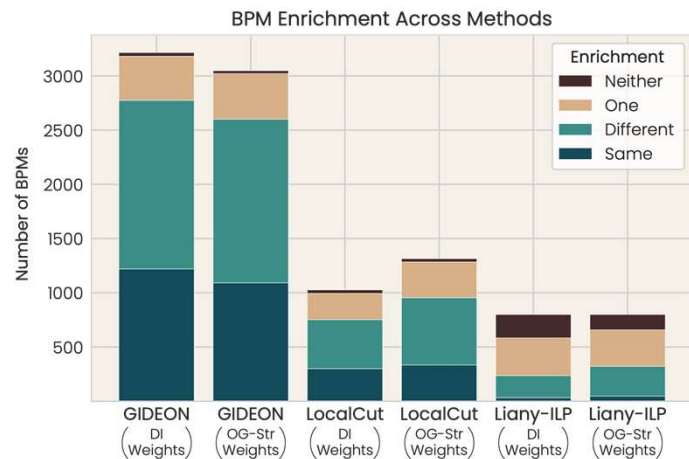


Output
Refinement

GIDEON outperforms all previous methods

Nearly triples the number of BPMs of LocalCut, the closest competitor, with stronger enrichment

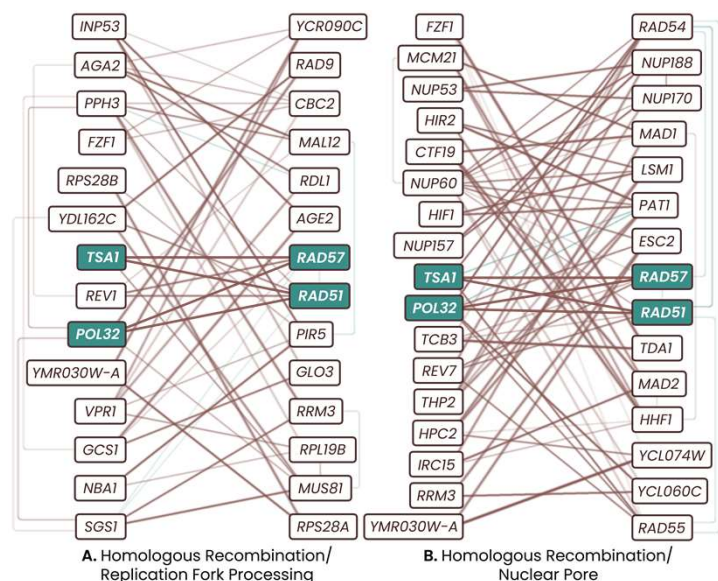
GIDEON with DI weights outperform OG-Str without additional experimental data



Unique BPMs from GIDEON

GIDEON identifies both BPMs on the right, highlighting the role of the overlapping genes in shared yet distinct processes

By removing edges from the network before searching again, Liany-ILP *cannot find* BPMs with overlapping interactions

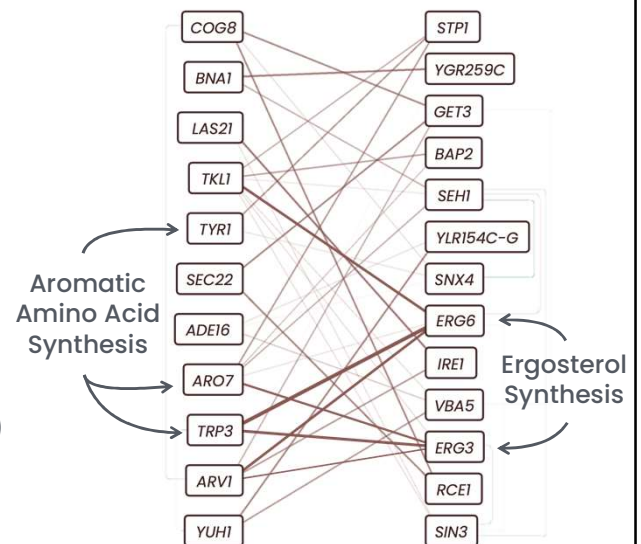


Insight Into Antifungal Drug Design

Ergosterol is a critical fungal cell membrane steroid for stress adaptation

Aromatic amino acids are phenylalanine, tyrosine, tryptophan, and histidine

Previous work has suggested inhibitors of aromatic amino acid biosynthesis as antifungal drugs (via the shikimate pathway)

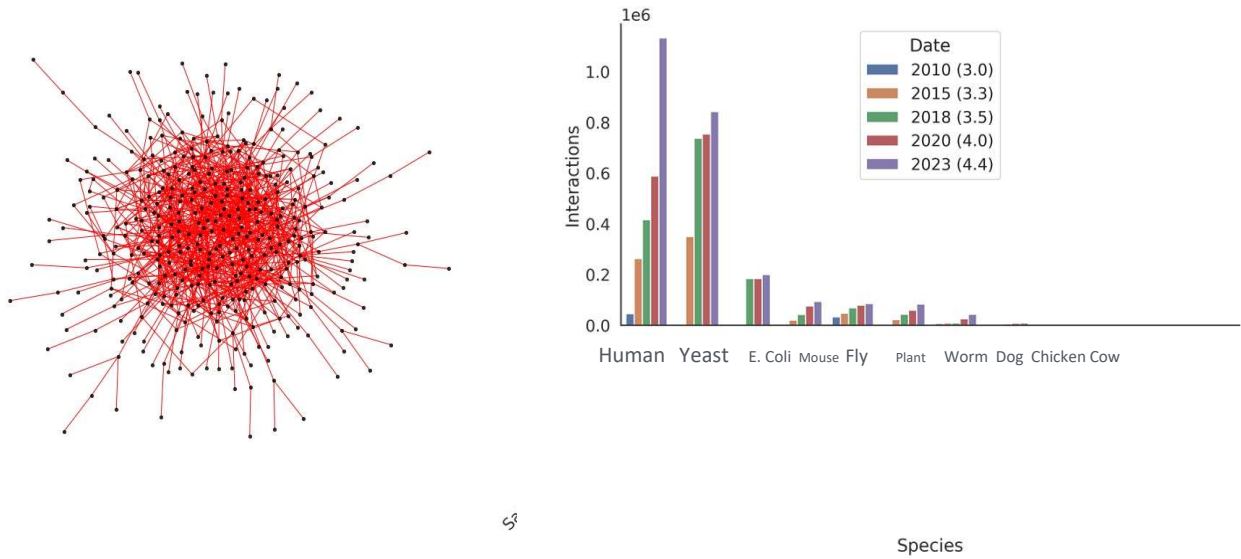


Memory-Efficient Blocked GPU

Parallel D-SCRIPT



Back to classical PPI networks: What data is available?



But: what about non-model organisms?

Coral Reefs Are Bleaching due to Climate Change/Heat Stress



Photo credit: Putnam Lab

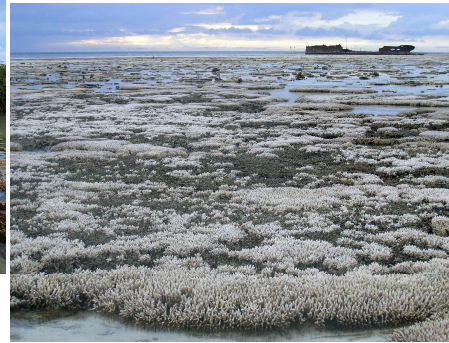
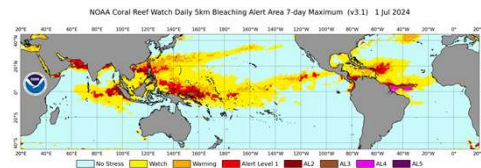


Photo credit: Oregon State University



NOAA: Daily Global 5km Satellite Coral Bleaching Heat Stress Alert Area

Coral **Animal** and Symbiont Genomes are now becoming available

Family	Species	Clade	Genome Size (Mb)	Scaffold #	Scaffold N50 kb	Gene #	BUSCO Completeness (genome assembly)	Reference(s)	Link
Acroporidae	<i>Acropora acuminata</i>	Complex	395	3,291	1,005	21,904	C:91.5 S:89.8 D:1.7 F:1.4 M:7.1	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora avic</i>	Complex	439	3,821	1,089	22,491	C:89.2 S:88.2 D:1.0 F:1.8 M:9.0	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora cyathaea</i>	Complex	426	4,046	1,084	22,584	C:90.4 S:88.5 D:1.9 F:1.9 M:7.7	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora digitifera</i>	Complex	416	3,951	1,056	22,231	C:90.2 S:88.7 D:1.5 F:1.6 M:8.2	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora echinata</i>	Complex	401	2,002	1,917	21,554	C:87.7 S:86.4 D:1.3 F:2.5 M:9.8	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora florida</i>	Complex	442	6,979	761	21,217	C:88.6 S:86.2 D:2.4 F:2.6 M:8.6	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora gemmifera</i>	Complex	401	2,274	1,541	21,563	C:88.6 S:87.5 D:1.3 F:1.6 M:8.4	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora hyacinthina</i>	Complex	447	2,758	1,284	22,464	C:90.7 S:87.8 D:2.9 F:1.5 M:7.8	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora intermedia</i>	Complex	417	6,294	977	22,891	C:90.6 S:87.9 D:1.7 F:1.4 M:8.0	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora microphyllina</i>	Complex	384	4,878	1,061	22,016	C:88.6 S:86.9 D:1.7 F:2.6 M:8.8	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora millepora</i>	Complex	475	954	19,846	26,188	C:86.0 S:79.0 D:0.4 F:1.5 M:8.1	Fujita et al. (2020)	https://www.sciencedirect.com/science/article/pii/S1537511920300474
Acroporidae	<i>Acropora millepora</i>	Complex	387	3,869	494	19,710	C:91.1 S:89.5 D:1.8 F:1.5 M:7.2	Ying et al. (2019)	https://academic.oup.com/igb/article/12/12/1374/548306
Acroporidae	<i>Acropora muricata</i>	Complex	421	6,861	975	21,201	C:88.3 S:87.5 D:1.5 F:1.2 M:8.5	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora nuda</i>	Complex	416	4,717	1,051	22,545	C:90.5 S:88.4 D:1.4 F:1.7 M:7.8	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora panama</i>	Complex	391	5,816	657	20,616	C:87.6 S:86.8 D:1.2 F:1.5 M:8.9	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora tenuis</i>	Complex	401	1,538	1,166	22,802	C:90.5 S:89.4 D:1.3 F:1.8 M:7.7	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Acropora variegata</i>	Complex	438	1,050	1,013	21,044	C:88.6 S:86.2 D:2.4 F:2.6 M:8.6	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Alcyonacea myriophyllina</i>	Complex	371	1,449	1,434	19,712	C:89.1 S:87.7 D:1.6 F:1.6 M:8.1	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Montipora castus</i>	Complex	653	4,925	899	21,983	C:88.5 S:86.7 D:1.8 F:2.7 M:8.8	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Acroporidae	<i>Montipora capitata</i>	Complex	885	3,961	940	18,229	C:90.4 F:1.2	Shimizu et al. (2019)	https://doi.org/10.1093/iob/obz018
Acroporidae	<i>Montipora capitata</i>	Complex	634	27,885	381	16,691	C:82.1 S:80.9 D:1.2 F:6.6 M:11.3	Heimkamp et al. (2019)	https://academic.oup.com/igb/article/12/12/1374/548306
Acroporidae	<i>Montipora effracilis</i>	Complex	641	5,162	1,132	19,170	C:86.4 S:84.6 D:1.4 F:1.7 M:10.9	Shimizu et al. (2021)	https://academic.oup.com/mbe/article/38/12/16/5900072
Poritidae	<i>Porites lutea</i>	Complex	552	2975	667	31,126	48% CE/OMA	Robison et al. (2019)	https://doi.org/10.1093/iob/obz018
Poritidae	<i>Porites rufa</i>	Complex	470	14,882	137	19,451	C:77.8 S:67.7 D:0.2 F:2.7 M:17.5%	Cole et al. (2018)	https://www.sciencedirect.com/science/article/pii/S0959268820300375
Agariciidae	<i>Pachypora speciosa</i>	Robust	984	2,968	766.6	39,160	C:90.5 P:5.1%	Bongers et al. (2021)	https://www.sciencedirect.com/science/article/pii/S0959268820300375
Euphyllidae	<i>Gastrea fascicularis</i>	Robust	334	11,029	87	22,428	C:68 P:8 M:23	Ying et al. (2019)	https://doi.org/10.1101/120598
Fungiididae	<i>Fungia spp.</i>	Robust	656	7624	813	38,209	C:65 F:32 M:22	Ying et al. (2019)	https://doi.org/10.1101/120598
Muriceidae	<i>Oribitella aemulans</i>	Robust	NA	NA	NA	NA	NA	Prada et al. (2016)	https://www.sciencedirect.com/science/article/pii/S0959268820300375
Muriceidae	<i>Oribitella fraxinea</i>	Robust	486	1,912	1,482	19,564	C:85.3 S:83.2 D:0.4 F:4.5 M:9.7	Prada et al. (2016)	https://www.sciencedirect.com/science/article/pii/S0959268820300375
Muriceidae	<i>Oribitella fraxinea</i>	Robust	NA	NA	NA	NA	NA	Prada et al. (2016)	https://www.sciencedirect.com/science/article/pii/S0959268820300375
Muriceidae	<i>Goniastrea aspera</i>	Robust	796	1,996	918	15,505	C:68 P:8 M:23	Ying et al. (2019)	https://doi.org/10.1101/120598
Montastreae	<i>Montastrea cavernosa</i>	Robust	448	5,681	343	41,577	C:81.4 F:9.8	Rippe et al. (2021)	https://onlinelibrary.wiley.com/doi/10.1111/mec.15931
Pocilloporidae	<i>Pocillopora acuta</i>	Robust	404	550	1,096	16,704	C:75.6 S:68.3% D:1.9% F:1.1% M:2.8%	Stephens et al. (2021)	https://www.biorxiv.org/content/10.1101/2021.11.21.46947v2
Pocilloporidae	<i>Pocillopora damicornis</i>	Robust	234	4,902	306	19,933	C:89.2 S:88.7 D:0.5 F:1.2 M:8.4	Cunningham et al. (2018)	https://doi.org/10.1093/iob/obz018
Pocilloporidae	<i>Pocillopora verrucosa</i>	Robust	380	18,038	311	27,439	C:82.2 S:69.0 D:0.2 F:1.7 P:1.4 M:1.5 R:9%	Bullago-Lopez et al. (2020)	https://doi.org/10.1093/iob/obz018
Pocilloporidae	<i>Pocillopora verticillata</i>	Robust	400	1,887	617	29,491	C:88.1 S:86.8 D:1.5 F:1.3 M:8.4	Watanabe et al. (2017)	https://doi.org/10.1093/iob/obz018

From Cowen and Putnam, Annual Reviews of Biomedical Science, 2022

Species	Clade	Genome size (Mb)	Gene #	URL
Pocillopora damnicornis	Robust	234	19,935	https://doi.org/10.1038/s41598-018-34459-8

Coral Animal and **Symbiont** Genomes are now becoming available

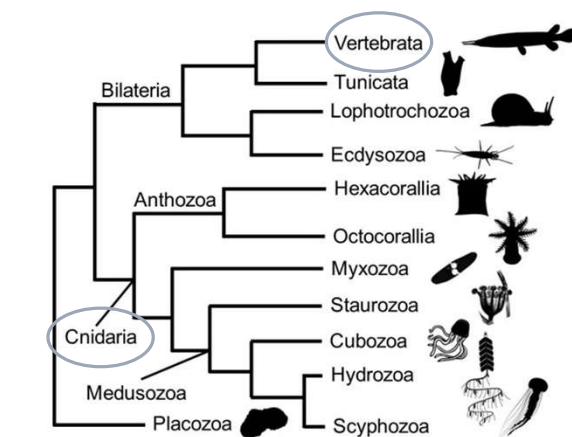
Family	Species	Genome Size (Mb)	Gene #	Reference(s)
Symbiodiniaceae	Breviolum minutum	616	41,925	Shoguchi et al. (2013)
Symbiodiniaceae	Cladocopium sp. C92	705	65,832	Shoguchi et al. (2018)
Symbiodiniaceae	Cladocopium goreau	1028	35,913	Liu et al. (2018)
Symbiodiniaceae	Durudinium trenchii	670	30,054	Shoguchi et al. (2021)
Symbiodiniaceae	Fugacium kawagutii (V3)	937	45,192	Aranda et al. (2016)
Symbiodiniaceae	Symbiodinium fitti	602	37,621	Reich et al. (2021)
Symbiodiniaceae	Symbiodinium microadriaticum	808	49,109	Aranda et al. (2016)
Symbiodiniaceae	S. microadriaticum CassKB8	1120	42,652	Gonzalez-Pech et al. (2021)
Symbiodiniaceae	S. microadriaticum 04-503SCI.03	1053	38,462	Gonzalez-Pech et al. (2021)
Symbiodiniaceae	S. tridacnidorum CCMP2592*	1287	45,474	Gonzalez-Pech et al. (2021)
Symbiodiniaceae	S. linucheae CCMP2456	915	32,053	Gonzalez-Pech et al. (2021)
Symbiodiniaceae	S. necropappetens CCMP2469	1007	35,672	Gonzalez-Pech et al. (2021)
Symbiodiniaceae	S. natans CCMP2548*	740	35,270	Gonzalez-Pech et al. (2021)
Symbiodiniaceae	S. pilosum CCMP2461	1994	23,437	Gonzalez-Pech et al. (2021)
Symbiodiniaceae	Symbiodinium tridacnidorum	767	69,018	Shoguchi et al. (2018)

From Cowen and Putnam, Annual Reviews of Biomedical Science, 2022

Family	Species	Genome size (Mb)	Gene #	Reference
Symbiodiniaceae	Cladocopium goreau	1028	35,913	Liu et al (2018)

Corals very evolutionarily distant so protein sequences very different

For many coral proteins, you won't be able to find functionally annotated proteins that are good sequence matches..

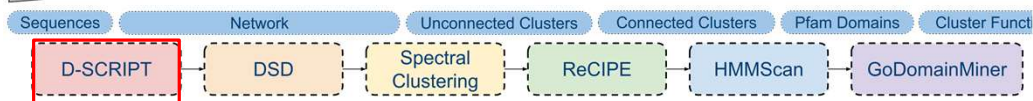
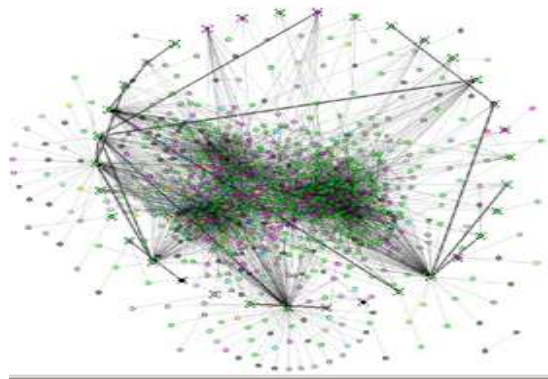


From: Vandepas et al, Biomolecules 2023, 13(5), 777;

Genome wide prediction of protein-protein interactions is the first step in the Philharmonic Pipeline



Organism
Complete
Proteome

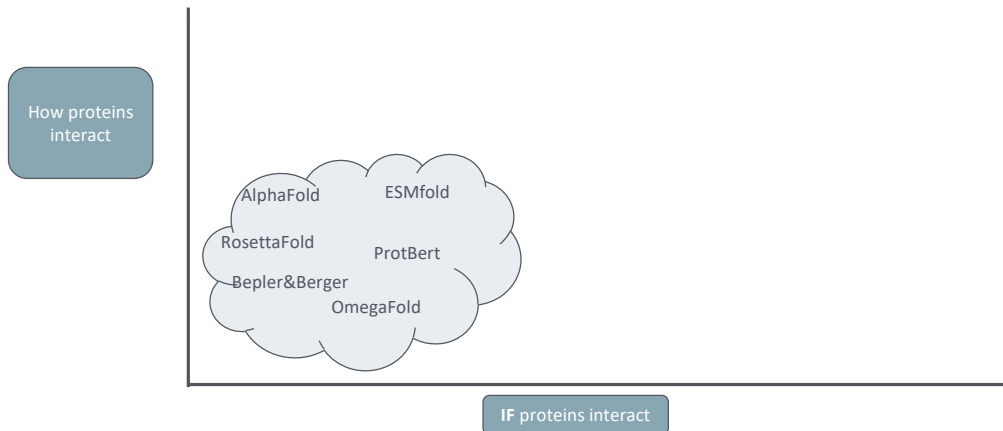


Leveraging language models for **lightweight** and **computationally efficient** PPI predictions

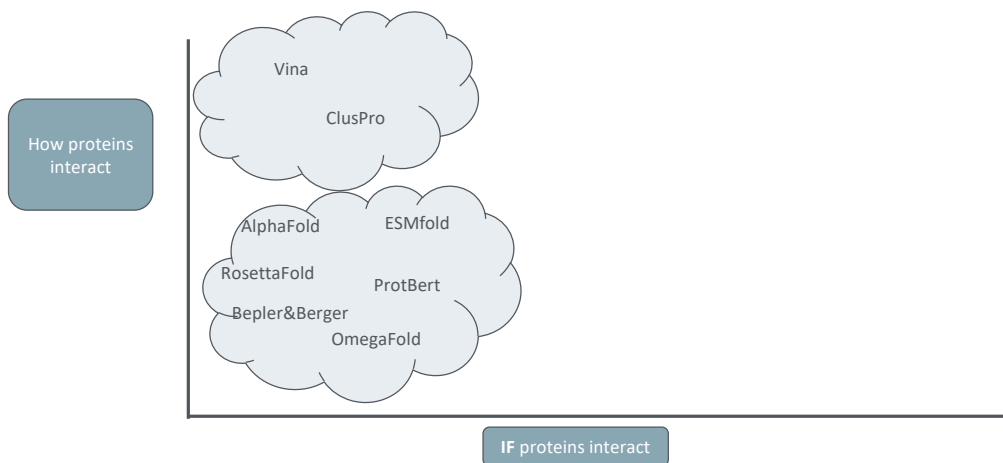
How proteins
interact

IF proteins interact

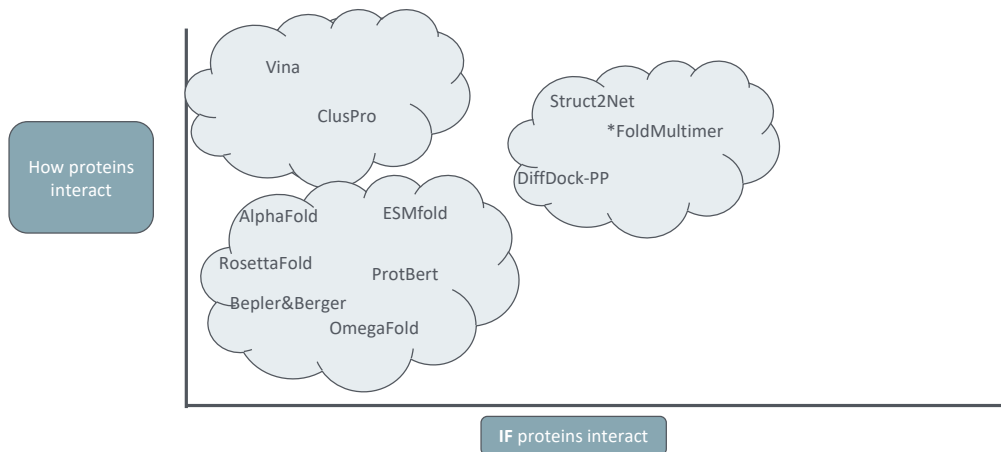
Leveraging language models for **lightweight** and **computationally efficient** PPI predictions



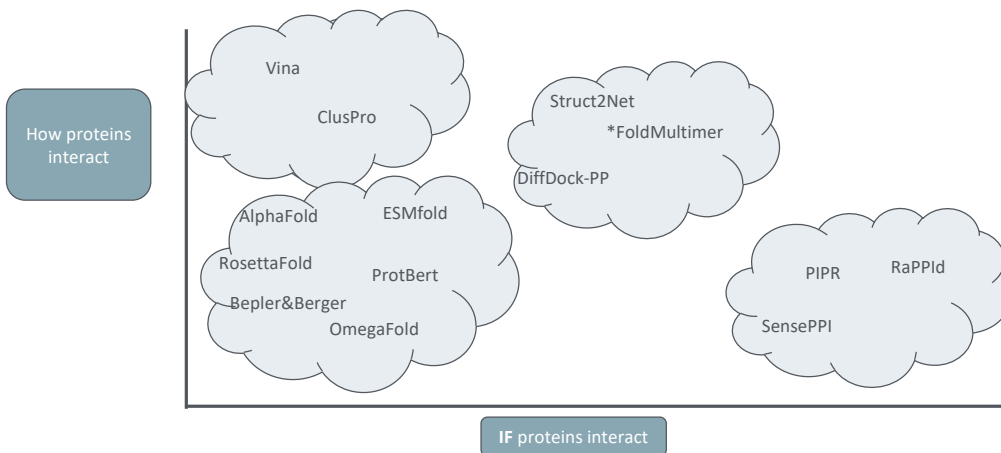
Leveraging language models for **lightweight** and **computationally efficient** PPI predictions



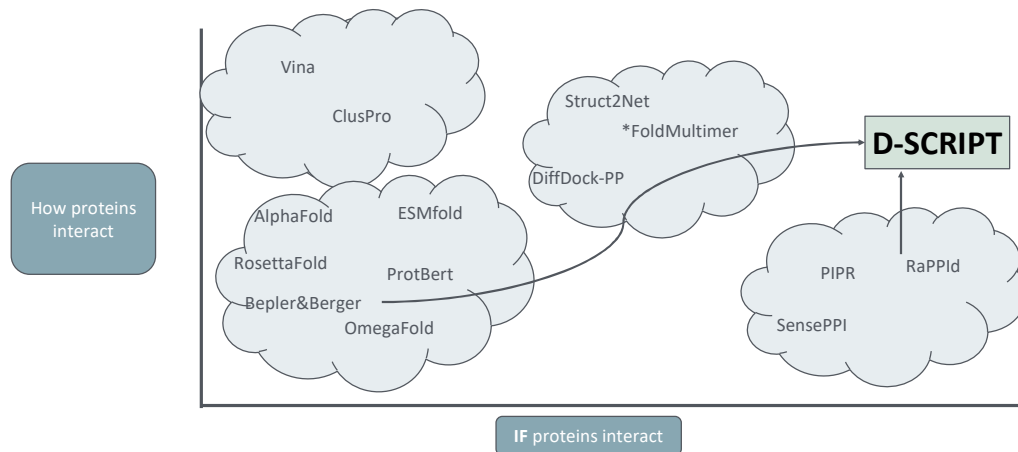
Leveraging language models for **lightweight** and **computationally efficient** PPI predictions



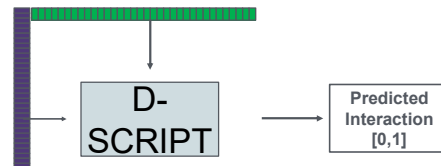
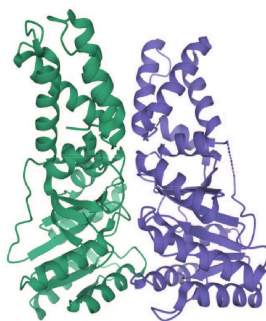
Leveraging language models for **lightweight** and **computationally efficient** PPI predictions



Leveraging language models for **lightweight** and **computationally efficient** PPI predictions



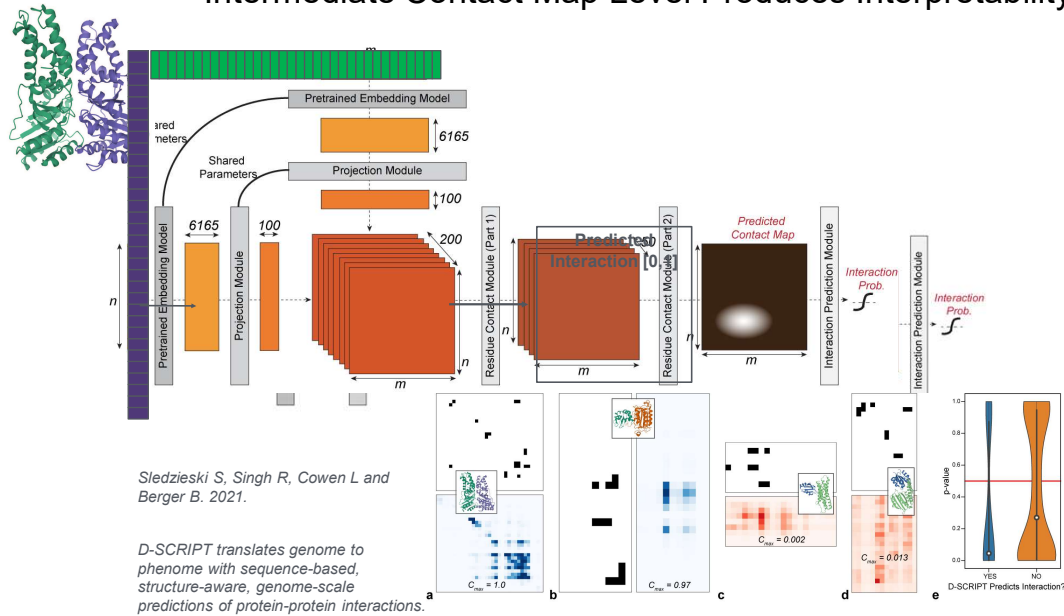
D-Script Is Trained on the Human Interactome, and Learns to Predict PPIs in A Different Species



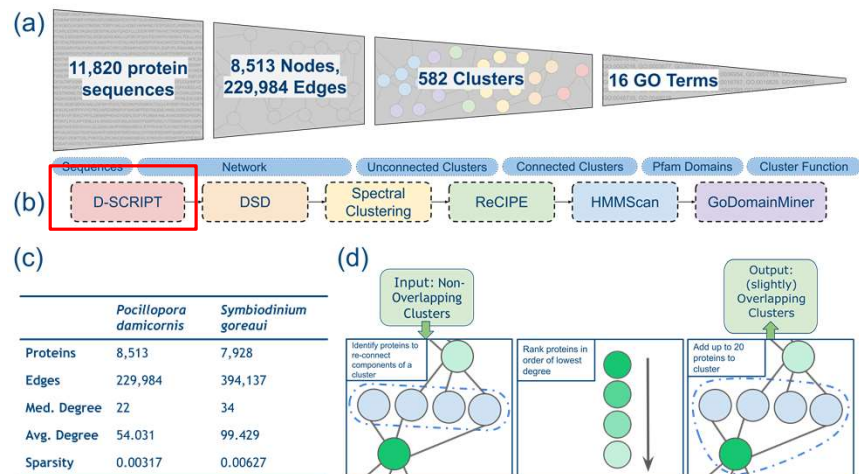
Sledzieski et al., 2021

Important to use a method that is lightweight
(only needs to predict the binary)

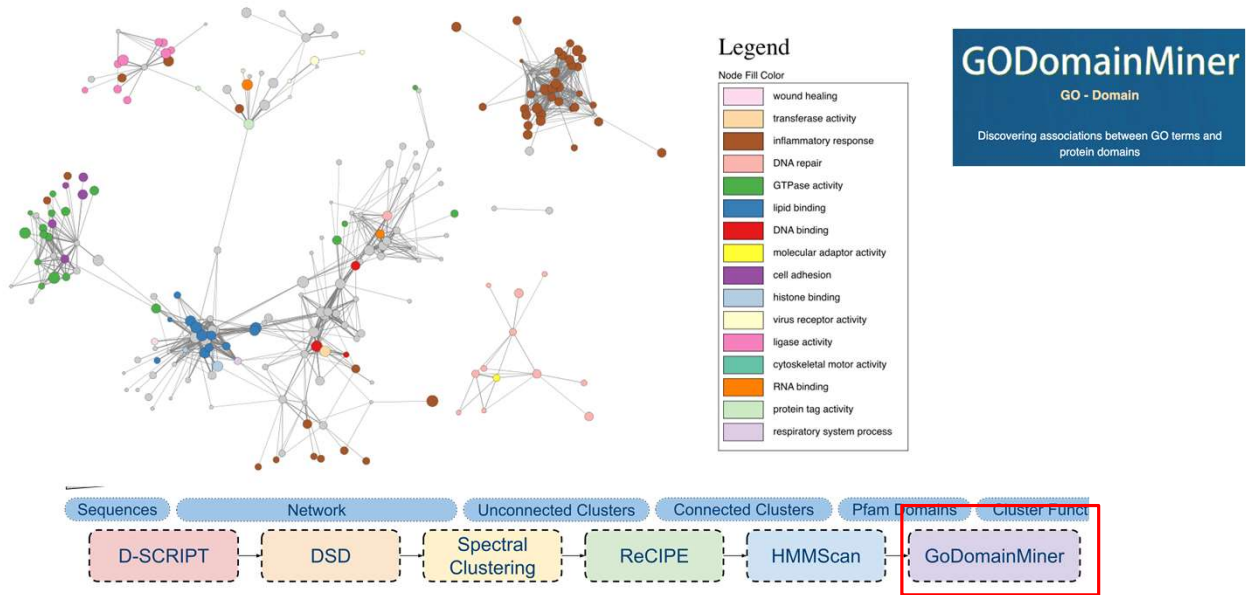
D-Script Can Predict PPIs Across Species: Intermediate Contact Map Level Produces Interpretability



D-SCRIPT is the first step in the PHILHARMONIC Pipeline



Pfam to GO mapping is used to assign functional labels to proteins (and clusters)



Leveraging language models for **lightweight** and **computationally efficient** PPI predictions

- Language models trained on a large corpus of proteins learn **general structural features** of proteins that can be used to predict interaction
- Maintain **speed** and ease of use of sequence-based deep learning methods

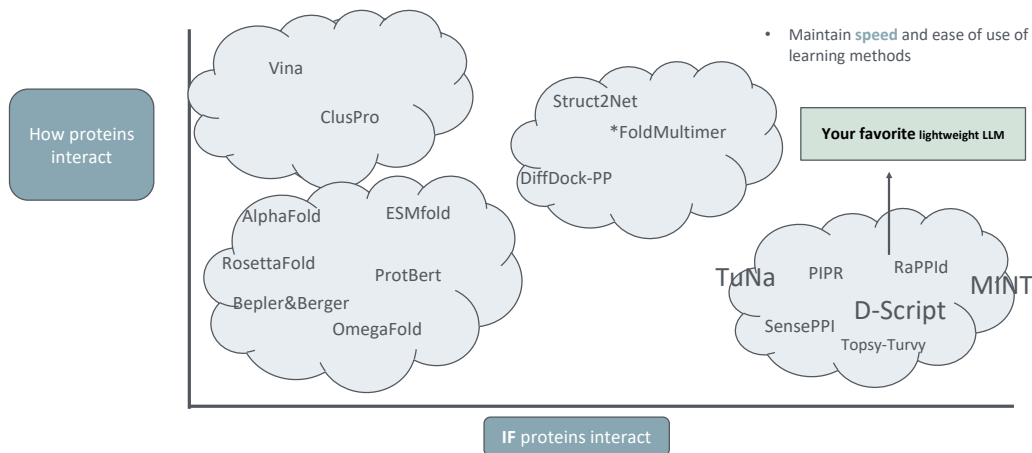


Figure 1. (A) The original serial version of D-SCRIPT iterates through each pair of candidate proteins. (B) This ...

Running D-SCRIPT
genome-wide:

If we load all
proteins
embeddings into
memory:

Very expensive!!

On the other hand,
if we fetch on
demand very slow!!

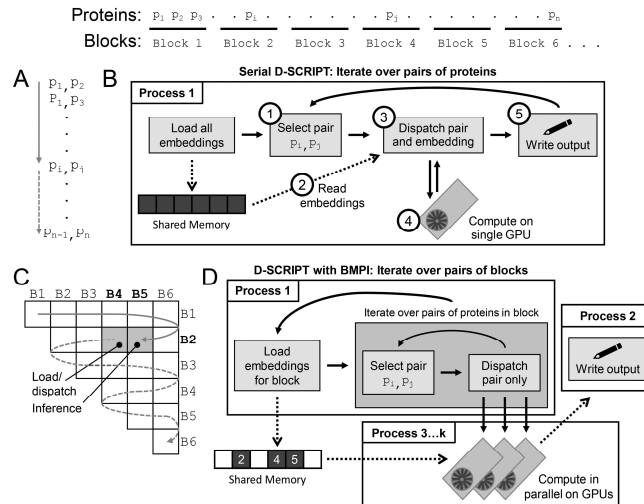


Figure 1. (A) The original serial version of D-SCRIPT iterates through each pair of candidate proteins. (B) This ...

Running D-SCRIPT
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Very expensive!!

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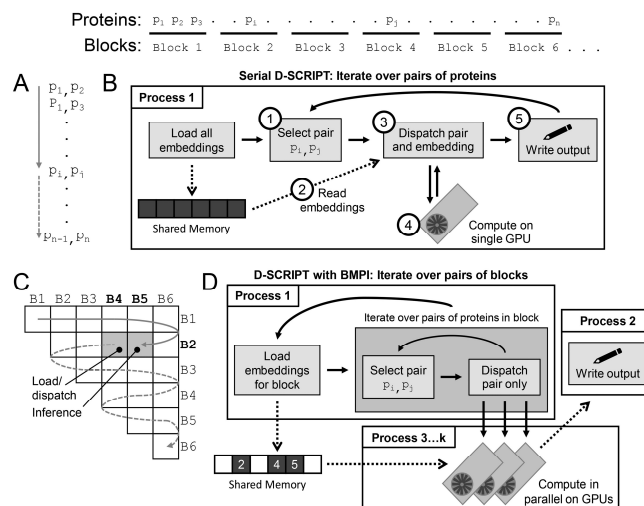
Solution: divide
proteins into blocks;

Solve combinatorial
problem of

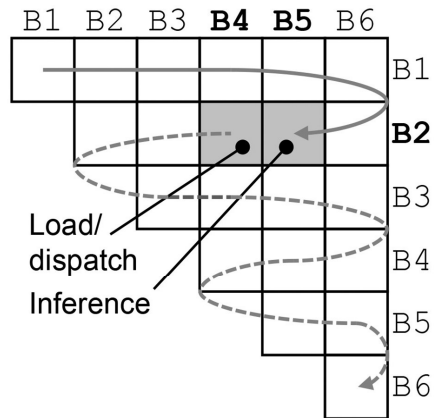
Choosing pairs so
that blocks do not

Have to be
frequently
loaded/unloaded

From memory



Example with 6 Blocks

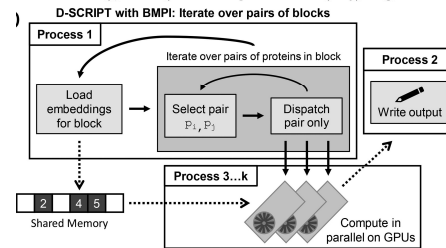


```

7:   if  $i = 0$  and  $blocks > 1$  then  $Embeds_3 \leftarrow LOAD(1)$  end if
8:   for  $j \in [i + 1, blocks]$  do
9:     if  $j = i + 1$  then
10:       $Embeds_2 \leftarrow Embeds_3$ 
11:      if  $j \neq blocks - 2$  then  $Embeds_3 = \emptyset$  end if
12:    else
13:       $Embeds_2 \leftarrow LOAD(j, flag : (cp - 1))$ 
14:    end if
15:     $cp \leftarrow cp + 1$ 
16:    SUBMIT_PAIR( $i, j, Embeds_1, Embeds_2, flag : cp$ )
17:  end for
18: else
19:   if  $i = blocks - 1$  then
20:      $Embeds_1 \leftarrow Embeds_2$ 
21:   else if  $i = blocks - 2$  then
22:      $Embeds_1 \leftarrow Embeds_3$ 
23:   else
24:      $Embeds_1 \leftarrow LOAD(i, flag : (cp - 1))$ 
25:   end if
26:   for  $j \in [blocks - 1, i + 2]$  do
27:      $cp \leftarrow cp + 1$ 
28:     SUBMIT_PAIR( $i, j, Embeds_1, Embeds_2, flag : cp$ )
29:      $Embeds_2 \leftarrow LOAD(j - 1, flag : (cp - 1))$ 
30:   end for
31:   if  $i < blocks - 2$  then
32:     SUBMIT_PAIR( $i, i + 2, Embeds_1, Embeds_2$ )
33:      $cp \leftarrow cp + 1$ 
34:      $Embeds_3 \leftarrow Embeds_2$ 
35:   end if
36:   SUBMIT_SELF( $i, Embeds_1$ )

```

7: $\triangleright$ Incrementing inner iteration
 10: $\triangleright$ Reuse previously-loaded data
 18: $\triangleright$ Special case to reuse loaded embeddings in the final iteration
 26: $\triangleright$ Decrementing inner iteration
 31: $\triangleright$ Special cases to re-use loaded embeddings
 36: $\triangleright$ Self-pair submission ($i = j$) using loaded embeddings



Benchmarking Results

Dataset: DMe150: Take complete Fly proteome; first isoform from each protein; remove proteins

With more than 1000 residues; randomly sample half. Gives: 6282 proteins (19 728 621 pairs)

Server config: 2 AMD EPYC 7502 processors, 2TB of RAM, and 8 NVIDIA A6000 GPUs

Benchmarking Results

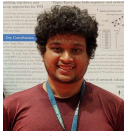
Dataset: DMel50: Take complete Fly proteome; first isoform from each protein; remove proteins

With more than 1000 residues; randomly sample half. Gives: 6282 proteins (19 728 621 pairs)

Server config: 2 AMD EPYC 7502 processors, 2TB of RAM, and 8 NVIDIA A6000 GPUs

Method	GPUs	Blocks	Time (Hours)	Est. Memory (GB)
Original D-SCRIPT	1	N/A	52.06	61.10
Blocked D-SCRIPT	8	1	6.42	87.97
Blocked D-SCRIPT	1	64	50.91	8.39
Blocked D-SCRIPT	4	64	12.82	19.48
Blocked D-SCRIPT	8	64	6.62	34.55





Kapil Devkota



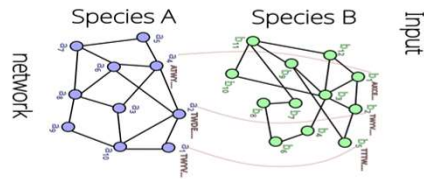
Anselm Blumer



Xiaozhe Hu



Devkota, K., Blumer, A., Hu, X., & Cowen, L. (2024). Approximate IsoRank for Scalable and Functionally Meaningful Cross-Species Alignments of Protein Interaction Networks. *Journal of Computational Biology*, 31(10), 990-1007.



Garcia, J.J., Kevin, M.Y., Freudenreich, C.H. and Cowen, L.J., 2026. A Novel ILP Framework to Identify Compensatory Pathways in Genetic Interaction Networks with GIDEON. *bioRxiv*.



Jocelyn Garcia



Freudenreich



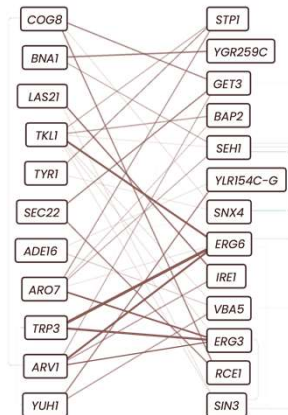
Kevin Yu

NSF-2149871

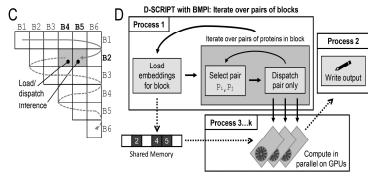
NIH-R01GM163241



NIH-R01GM163241



Schäffer, D. E., Sledzieski, S., Cowen, L., & Berger, B. (2025). Memory-efficient, accelerated protein interaction inference with blocked, multi-GPU D-SCRIPT. *Bioinformatics*, 41(10), btaf564.



NSF-2141064



Daniel Schäffer



Sam Sledzieski



Bonnie Berger

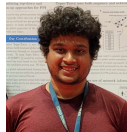
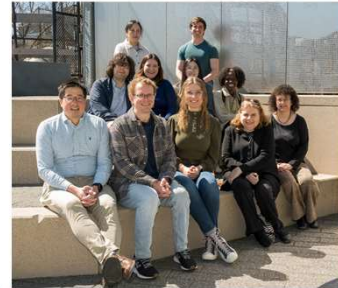


NIH
1R35GM14186

Tufts
UNIVERSITY



NIH-R01GM163241



Kapil Devkota



Anselm Blumer



Xiaozhe Hu

NIH-R01GM163241



Jocelyn Garcia

Catherine
Freudenreich

Kevin Yu

NSF-2149871

NSF-2141064



Daniel Schäffer



Sam Sledzieski



Bonnie Berger

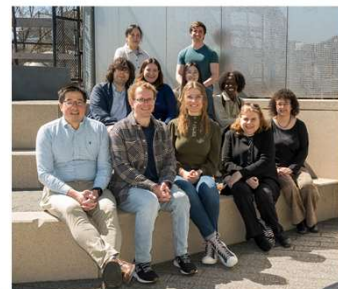


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1R35GM14186

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THANK YOU!!!