

$$S = \max_{\ell} S(\ell).$$