An Information Theoretic Approach to Validate Deep Learning-Based Algorithms

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Workshop on Safety and Security of Deep Learning ICERM (virtual), April 10 – 11, 2021







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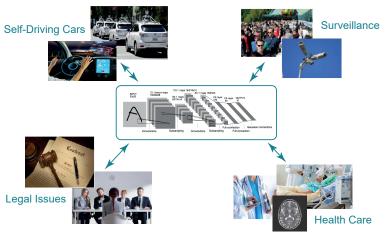
Cinjon Resnick (NYU Courant)



Joan Bruna (NYU Courant)

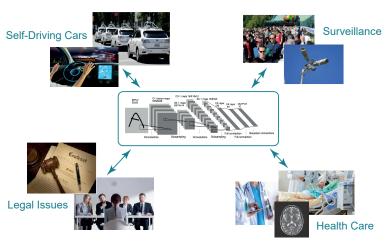


The Dawn of Deep Learning





The Dawn of Deep Learning



Deep Neural Networks still act as a Black Box!



Deep Learning = Alchemy? ... Safety?



"Ali Rahimi, a researcher in artificial intelligence (AI) at Google in San Francisco, California, took a swipe at his field last December—and received a 40-second ovation for it. Speaking at an AI conference, Rahimi charged that machine learning algorithms, in which computers learn through trial and error, have become a form of "alchemy." Researchers, he said, do not know why some algorithms work and others don't, nor do they have rigorous criteria for choosing one AI architecture over another.....

Science, May 2018





Theoretical Foundations of Deep Learning

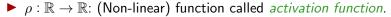


The Mathematics of Deep Neural Networks

Definition:

Assume the following notions:

- $ightharpoonup d \in \mathbb{N}$: Dimension of input layer.
- L: Number of layers.
- N: Number of neurons.

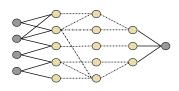


$$ightharpoonup T_\ell: \mathbb{R}^{N_{\ell-1}} o \mathbb{R}^{N_\ell}$$
, $\ell=1,\ldots,L$: Affine linear maps.

Then $\Phi: \mathbb{R}^d \to \mathbb{R}^{N_L}$ given by

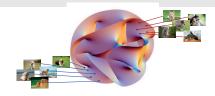
$$\Phi(x) = T_L \rho(T_{L-1} \rho(\dots \rho(T_1(x))), \quad x \in \mathbb{R}^d,$$

is called (deep) neural network (DNN).



High-Level Set Up:

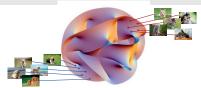
► Samples $(x_i, f(x_i))_{i=1}^m$ of a function such as $f: \mathcal{M} \to \{1, 2, \dots, K\}$.



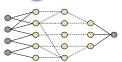


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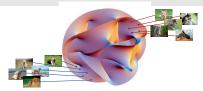
Select an architecture of a deep neural network, i.e., a choice of d, L, $(N_{\ell})_{\ell=1}^{L}$, and ρ . Sometimes selected entries of the matrices $(A_{\ell})_{\ell=1}^{L}$, i.e., weights, are set to zero at this point.



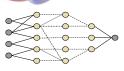


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▶ Learn the affine-linear functions $(T_{\ell})_{\ell=1}^{L} = (A_{\ell} \cdot + b_{\ell})_{\ell=1}^{L}$ by

$$\min_{(A_\ell,b_\ell)_\ell} \sum_{i=1}^m \mathcal{L}(\Phi_{(A_\ell,b_\ell)_\ell}(x_i),f(x_i)) + \lambda \mathcal{R}((A_\ell,b_\ell)_\ell)$$

yielding the network $\Phi_{(A_\ell,b_\ell)_\ell}: \mathbb{R}^d \to \mathbb{R}^{N_L}$,

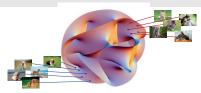
$$\Phi_{(A_{\ell},b_{\ell})_{\ell}}(x) = T_{L}\rho(T_{L-1}\rho(\ldots\rho(T_{1}(x))).$$

This is often done by stochastic gradient descent.

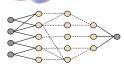


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Interpretability:

- Why did a trained deep neural network reach a certain decision?
- Which components of the input do contribute most?
- → Information Theory, Uncertainty Quantification, ...



Interpretability



General Problem Setting

Question:

- Given a trained neural network.
- We don't know what the training data was nor how it was trained.
- → Can we determine how it operates?

Opening the Black Box!





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- Assume a job application is rejected.
- Imagine this rejection was done by a neural network-based algorithm.
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Vision for the Future:

Explanation of a decision indistinguishable from a human being!



- Gradient based methods:
 - Sensitivity Analysis (Baehrens, Schroeter, Harmeling, Kawanabe, Hansen, Müller, 2010)
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- Game theoretic methods:
 - Shapley values (Shapley, 1953), (Kononenko, Štrumbeli. 2010)
 - ► SHAP (Shapley Additive Explanations) (Lundberg, Lee, 2017)



What is Relevance?

Main Goal: We aim to understand decisions of "black-box" predictors!

map for digit 3 map for digit 8





Classification as a Classical Task for Neural Networks:

- Which features are most relevant for the decision?
 - Treat every pixel separately
 - Consider combinations of pixels
 - Incorporate additional knowledge
- How certain is the decision?



- What exactly is relevance in a mathematical sense?
- ► What is a good relevance map?
- How to compare different relevance maps?
- ► How to extend to challenging modalities?



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- How to compare different relevance maps?
 - → Canonical framework for comparison.
- How to extend to challenging modalities?
 - → Conceptually general and flexible interpretability approach.



The Relevance Mapping Problem



The Relevance Mapping Problem

The Setting: Let

- \bullet $\Phi: [0,1]^d \to [0,1]$ be a classification function,
- \triangleright $x \in [0,1]^d$ be an input signal.



$$\xrightarrow{\Phi} \Phi(x) = 0.97$$

"Monkey"



$$\longrightarrow \Phi \qquad \qquad \Phi(x) = 0.07$$

"Not a monkey"



The Relevance Mapping Problem

The Task:

- \triangleright Determine the most relevant components of x for the prediction $\Phi(x)$.
- ▶ Choose $S \subseteq \{1, ..., d\}$ of components that are considered relevant.
- S should be small (usually not everything is relevant).
- \triangleright S^c is considered non-relevant.



Original image x



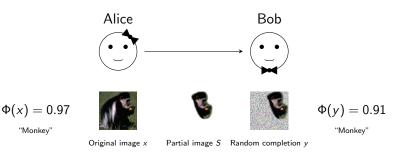
Relevant components S



Non-relevant components Sc



Rate-Distortion Viewpoint



Obfuscation: Let

- $ightharpoonup n \sim \mathcal{V}$ be a random noise vector, and
- \triangleright y be a random vector defined as $y_S = x_S$ and $y_{S^c} = n_{S^c}$.



Rate-Distortion Viewpoint

Recall: Let

- $lackbox{ }\Phi: [0,1]^d \rightarrow [0,1] \text{ be a classification function, }$
- \triangleright $x \in [0,1]^d$ be an input signal,
- $ightharpoonup n \sim \mathcal{V}$ be a random noise vector, and
- \triangleright y be a random vector defined as $y_S = x_S$ and $y_{S^c} = n_{S^c}$.

Expected Distortion:

$$D(S) = D(\Phi, x, S) = \mathbb{E}\left[\frac{1}{2}(\Phi(x) - \Phi(y))^2\right]$$

Rate-Distortion Function:

$$R(\epsilon) = \min_{S \subseteq \{1,\dots,d\}} \{|S| : D(S) \le \epsilon\}$$

 \rightarrow Use this viewpoint for the definition of a relevance map!

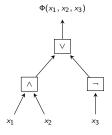


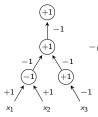
Finding a minimizer of $R(\epsilon)$ or even approximating it is very hard!



Hardness Results

Boolean Functions as ReLU Neural Networks:





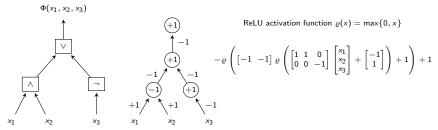
ReLU activation function $\varrho(x) = \max\{0, x\}$

$$-\varrho\left(\begin{bmatrix} -1 & -1 \end{bmatrix}\varrho\left(\begin{bmatrix} 1 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} -1 \\ 1 \end{bmatrix}\right) + 1\right) + 1$$



Hardness Results

Boolean Functions as ReLU Neural Networks:



The Binary Setting: Let

- ullet $\Phi: \{0,1\}^d \to \{0,1\}$ be classifier functions,
- \triangleright $x \in \{0,1\}^d$ be signals, and
- $\triangleright \mathcal{V} = \mathcal{U}(\{0,1\}^d)$ be a uniform distribution.



Hardness Results

We consider the binary case.

Theorem (Wäldchen, Macdonald, Hauch, K, 2019): Given Φ , x, $k \in \{1, \ldots, d\}$, and $\epsilon < \frac{1}{4}$. Deciding whether $R(\epsilon) \le k$ is NP^{PP}-complete.

Finding a minimizer of $R(\epsilon)$ is hard!



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Theorem (Wäldchen, Macdonald, Hauch, K, 2019):

Given Φ , x, and $\alpha \in (0,1)$. Approximating $R(\epsilon)$ to within a factor of $d^{1-\alpha}$ is NP-hard.

Even the approximation problem of it is hard!



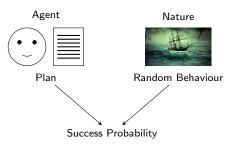
What is NPPP?

The Complexity Class NPPP:

Many important problems in artificial intelligence belong to this class.

Some Examples:

- Planning under uncertainties
- Finding maximum a-posteriori configurations in graphical models
- Maximizing utility functions in Bayesian networks





Our Method:

Rate-Distortion Explanation (RDE)



Problem Relaxation

Discrete problem	Continuous problem
$S \subseteq \{1, \dots, d\}$ $y_S = x_S, y_{S^c} = n_{S^c}$ $D(S)$ $ S $	



Problem Relaxation

	Discrete problem	Continuous problem
Relevant set	$S \subseteq \{1,\ldots,d\}$	$s \in [0,1]^d$
Obfuscation	$y_S = x_S, y_{S^c} = n_{S^c}$	$y = s \odot x + (1 - s) \odot n$
Distortion	D(S)	D(s)
Rate/Size	5	$\ s\ _1$



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Resulting Minimization Problem:

minimize
$$D(s) + \lambda ||s||_1$$
 subject to $s \in [0,1]^d$



Distortion:

$$D(s) = \mathbb{E}\left[\frac{1}{2}(\Phi(x) - \Phi(y))^{2}\right]$$
$$= \frac{1}{2}(\Phi(x) - \mathbb{E}[\Phi(y)])^{2} + \frac{1}{2}\operatorname{cov}[\Phi(y)]$$

Obfuscation:

$$\mathbb{E}[y] = s \odot x + (1 - s) \odot \mathbb{E}[n]$$

$$cov[y] = diag(1 - s) cov[n] diag(1 - s)$$



$$\mathbb{E}[y], \operatorname{cov}[y] \xrightarrow{\Phi} \mathbb{E}[\Phi(y)], \operatorname{cov}[\Phi(y)]$$



$$\mathbb{E}[y], \operatorname{cov}[y] \xrightarrow{\Phi} \mathbb{E}[\Phi(y)], \operatorname{cov}[\Phi(y)]$$

Generic Approach:

- Estimate using sample mean and sample covariance
- Possible for any classifier function Φ
- Might require large number of samples



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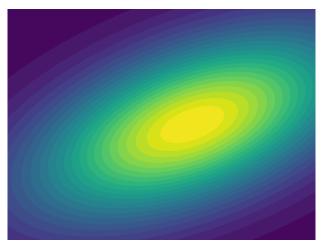
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Neural Network Approach:

- Use compositional structure of Φ
- Propagate distribution through the layers
- Project to simple family of distributions at each layer

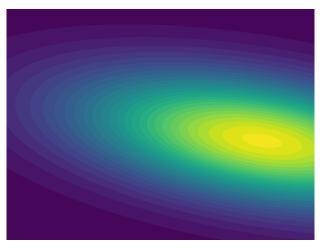


Input distribution: $\mathcal{N}(\mu_{\mathsf{in}}, \sigma_{\mathsf{in}})$



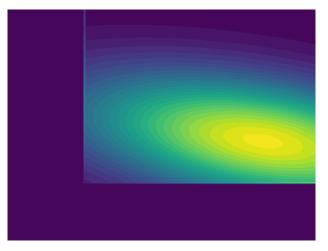


Affine transform: $\mathcal{N}(W\mu_{\mathsf{in}} + b, W\sigma_{\mathsf{in}}W^{\top})$



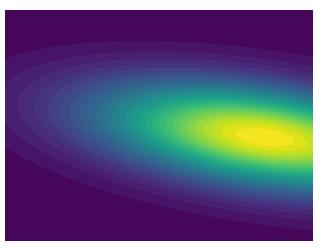


ReLU activation: Not Gaussian anymore





Moment matching output distribution: $\mathcal{N}(\mu_{\text{out}}, \sigma_{\text{out}})$





Numerical Experiments



MNIST Experiment



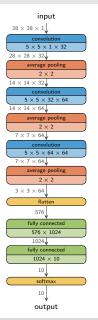
Data Set

 $28 \times 28 \times 1$ Image size

Number of classes 10

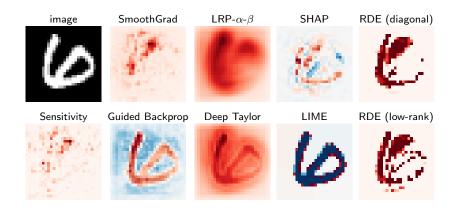
Training samples 50000

Test accuracy: 99.1%



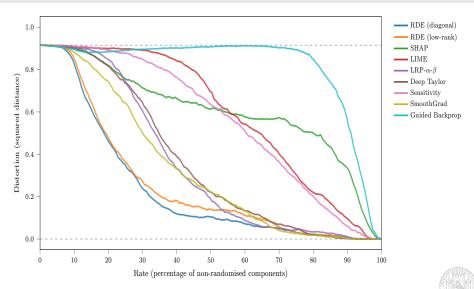


MNIST Experiment



SmoothGrad (Smilkov, Thorat, Kim, Viégas, Wattenberg, 2017), Layer-wise Relevance Propagation (Bach, Binder, Montavon, Klauschen, Müller, Samek, 2015), SHAP (Lundberg, Lee, 2017). Sensitivity Analysis (Simonyan, Vedaldi, Zisserman, 2013), Guided Backprop (Springenberg, Dosovitskiy, Brox, Riedmiller, 2015), Deep Taylor Decompositions (Montavon, Samek, Müller, 2018). LIME (Ribeiro, Singh, Guestrin, 2016)

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STL-10 Experiment









Data Set

Image size $96 \times 96 \times 3$

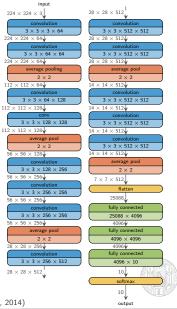
 $(224 \times 224 \times 3)$

Number of classes 10

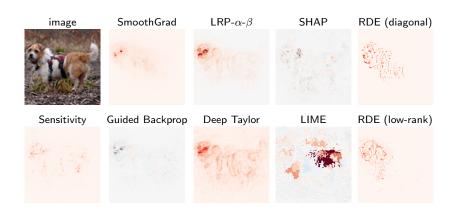
Training samples 4000

Test accuracy: 93.5%

(VGG-16 convolutions pretrained on Imagenet)

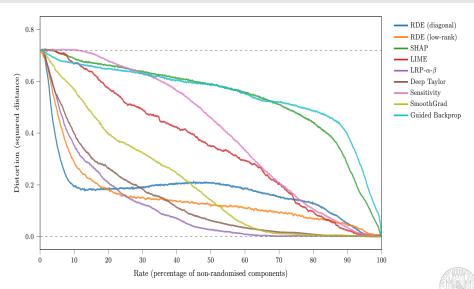


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Interpretable Machine Learning for Challenging Modalities



Desiderata

Problems:

- Modifying the image with random noise or some background color might lead to the obfuscation not being in the domain of the network.
 - → Does this give meaningful information about why the network made its decisions?
- The explanations are pixel-based.
 - → Does this lead to useful information for different modalities?





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Goal:

- ▶ Take the conditional data distribution into account.
- Ensure that specifics of various modalities can be handled.



Obfuscating Correctly

Recall for $s \in [0,1]^d$:

$$D(s) = \mathbb{E}_{y \sim \Upsilon_s} \left[\frac{1}{2} \left(\Phi(x) - \Phi(y) \right)^2 \right]$$



How do we obfuscate according to the conditional data distribution?



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How do we obfuscate according to the conditional data distribution?

Generative Transformation (Chang, Creager, Goldenberg, Duvenaud; '19):

- \blacktriangleright Let \mathcal{D} be the training data distribution.
- Use an inpainting network G so that a critic has trouble deciding whether the obfuscation

$$y := x \odot s + G(x, s, n) \odot (1 - s)$$

came from \mathcal{D} .

 \sim Sampling from the conditional data distribution $\mathcal{D}|_{v_s=x_s}$.



General Approach (Heiß, Levie, Resnick, K, Bruna; '20)

Optimization Problem:

We consider the following minimization problem:

$$\min_{s \in \{0,1\}^d} \mathbb{E}_{y \sim \Upsilon_s} \left[\frac{1}{2} (\Phi(x) - \Phi(y))^2 \right] + \lambda \|s\|_1,$$

where y is generated by a trained inpainting network G as

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Requirements of Different Modalities: Can be applied ...

- ... to images, but also audio data, etc.
- ▶ ... after a transform (e.g. a dictionary) to allow more complex features.

Conceptually general and flexible interpretability approach!



Audio Processing

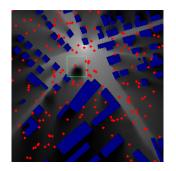
NSynth Dataset:

Instrument	Magnitude Importance	Phase Importance
Organ	0.829	1.0
Guitar	0.0	0.999
Flute	0.092	1.0
Bass	1.0	1.0
Reed	0.136	1.0
Vocal	1.0	1.0
Mallet	0.005	0.217
Brass	0.999	1.0
Keyboard	0.003	1.0
String	1.0	0.0

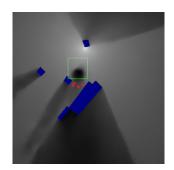


Telecommunication

RadioUNet (Levie, Cagkan, K, Caire; 2020):



Estimated map



Explanation



Conclusions



What to take Home...?

Deep Learning:

- ► A theoretical foundation of neural networks is largely missing: Expressivity, Learning, Generalization, and Interpretability.
- Deep neural networks act still as a black box.



Interpretability:

- Determining which input features are *most relevant* for a decision.
- We provide a precise mathematical notion for relevance based on rate-distortion theory.
- Computing the minimal rate is hard.
- ▶ We introduce a general and flexible interpretability approach for various modalities, based on a relaxed version.
- On classical examples, *outperforms current methods* for smaller rates.





THANK YOU!

References available at:

www.ai.math.lmu.de/kutyniok

Check related information on Twitter at:

@GittaKutyniok

Upcoming Book:

P. Grohs and G. Kutyniok Theory of Deep Learning
Cambridge University Press (in preparation)

